

CBSE Standard 12 Math Survival Guide-Differential Equations by Prof. Subhashish Chattopadhyay  
SKMClasses Bangalore Useful for I.Sc. PU-II AP-Maths IGCSE IB AP-Mathematics and other exams



## Spoon Feeding Differential Equations



**Simplified Knowledge Management Classes Bangalore**

My name is [Subhashish Chattopadhyay](#). I have been teaching for IIT-JEE, Various International Exams ( such as IMO [ International Mathematics Olympiad ], IPhO [ International Physics Olympiad ], IChO [ International Chemistry Olympiad ] ), IGCSE ( IB ), CBSE, I.Sc, Indian State Board exams such as WB-Board, Karnataka PU-II etc since 1989. As I write this book in 2016, it is my 25 th year of teaching. I was a Visiting Professor to BARC Mankhurd, Chembur, Mumbai, Homi Bhabha Centre for Science Education ( HBCSE ) Physics Olympics camp BARC Campus.

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**I am Life Member of ...**

- [IAPT \( Indian Association of Physics Teachers \)](#)
- [IPA \( Indian Physics Association \)](#)
- [AMTI \( Association of Mathematics Teachers of India \)](#)
- [National Human Rights Association](#)
- [Men's Rights Movement \( India and International \)](#)
- [MGTOW Movement \( India and International \)](#)

**And also of**

[IACT \( Indian Association of Chemistry Teachers \)](#)



**The selection for National Camp ( for Official Science Olympiads - Physics, Chemistry, Biology, Astronomy ) happens in the following steps ....**

1 ) **NSEP** ( National Standard Exam in Physics ) and **NSEC** ( National Standard Exam in Chemistry ) held around 24 rth November. Approx 35,000 students appear for these exams every year. The exam fees is Rs 100 each. Since 1998 the IIT JEE toppers have been topping these exams and they get to know their rank / performance ahead of others.

2 ) **INPhO** ( Indian National Physics Olympiad ) and **INChO** ( Indian National Chemistry Olympiad ). Around 300 students in each subject are allowed to take these exams. Students coming from outside cities are paid fair from the Govt of India.

3 ) The Top 35 students of each subject are invited at HBCSE ( Homi Bhabha Center for Science Education ) Mankhurd, near Chembur, BARC, Mumbai. After a 2-3 weeks camp the top 5 are selected to represent India. The flight tickets and many other expenses are taken care by Govt of India.

Since last 50 years there has been no dearth of “Good Books“. Those who are interested in studies have been always doing well. This e-Book does not intend to replace any standard text book. These topics are very old and already standardized.

### **There are 3 kinds of Text Books**

- The thin Books - Good students who want more details are not happy with these. Average students who need more examples are not happy with these. Most students who want to “Cram” quickly and pass somehow find the thin books “good” as they have to read less !!

- The Thick Books - Most students do not like these, as they want to read as less as possible. Average students are “busy” with many other things and have no time to read all these.

- The Average sized Books - Good students do not get all details in any one book. Most bad students do not want to read books of “this much thickness“ also !!

We know there can be no shoe that’s fits in all.

Printed books are not e-Books! Can’t be downloaded and kept in hard-disc for reading “later”  
.....

So if you read this book later, you will get all kinds of examples in a single place. This becomes a very good “Reference Material”. I sincerely wish that all find this “very useful”.

Students who do not practice lots of problems, do not do well. The rules of “doing well” had never changed .... Will never change !

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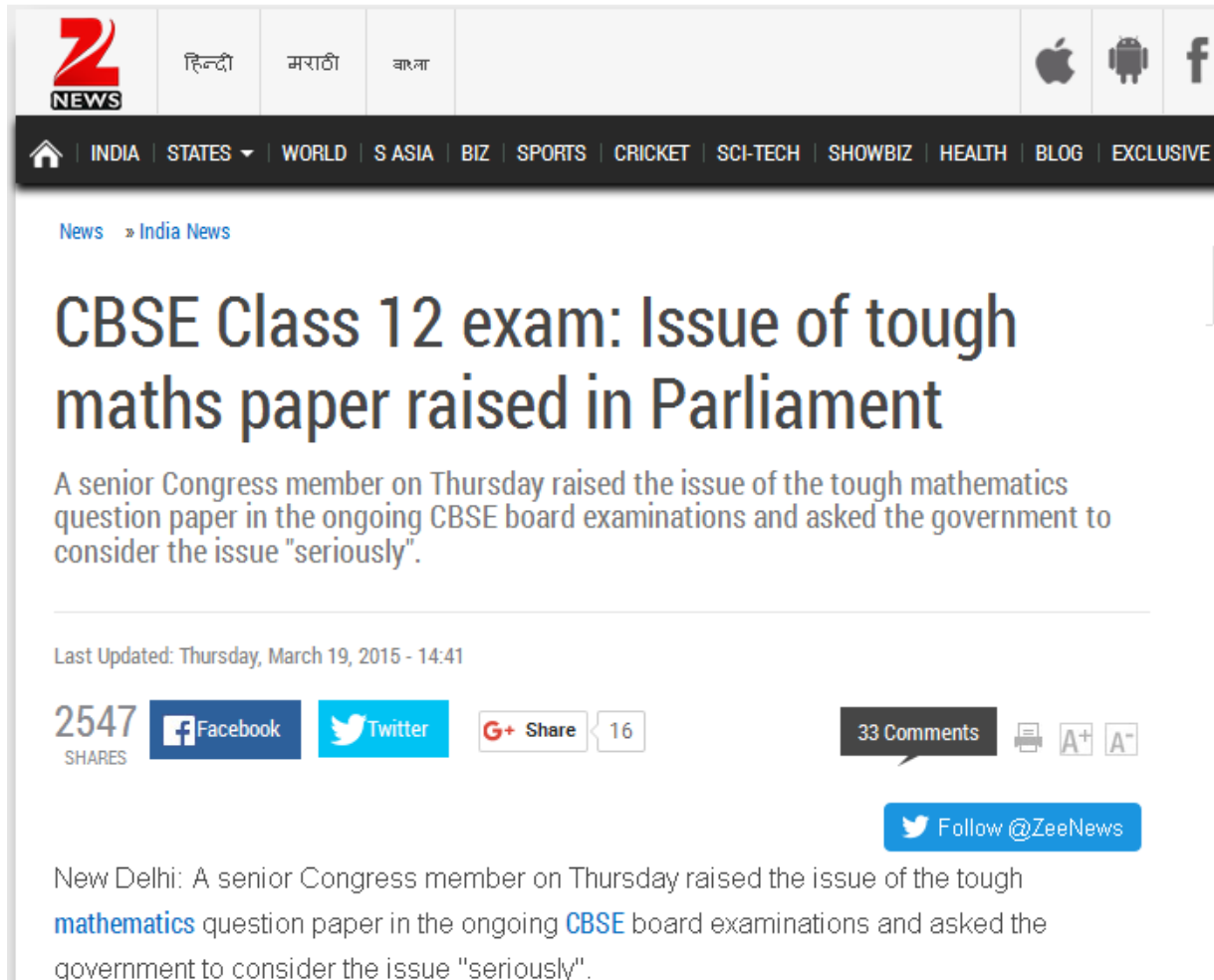
After 2016 CBSE Mathematics exam lots of students complained that the paper was tough!

The screenshot shows a news article on the IBNLIVE website. At the top, it says 'Updated 8:47 am Mar 22, 2016'. The website logo 'IBNLIVE' and 'CNN' are visible. Below the logo are language options: 'ENGLISH', 'HINDI', and 'MARATHI'. A navigation bar includes 'READ', 'WATCH', 'CRICKET', and 'TECH'. A secondary navigation bar lists 'LATEST', 'BUDGET 2016', 'POLITICS', 'INDIA', 'SPORTS', 'FOOTBALL', 'MOVIES', 'LIVE TV', 'BUZZ', and 'WC'. The article title is 'CBSE assures remedial measures for tricky and tough Class XII Math paper'. It is dated 'Posted on: 12:17 PM IST Mar 17, 2016 | Updated on: 12:20 pm, Mar 17, 2016 IST'. The article text states: 'After several students claimed that the Central Board of Secondary Education (CBSE) Class XII board Mathematics examination paper was 'tricky' and tough, the board has issued a clarification on remedial measures which are likely to be taken before evaluation. The CBSE says that feedback received from various stakeholders like students, subject teachers and examiners will be put before the committee of subject experts.'

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In 2015 also the same complain was there by many students



The screenshot shows a news article from Zee News. The header includes the Zee News logo, language options (Hindi, Marathi, Bangla), and mobile app icons (Apple, Android, Facebook). The navigation bar lists categories: INDIA, STATES, WORLD, S ASIA, BIZ, SPORTS, CRICKET, SCI-TECH, SHOWBIZ, HEALTH, BLOG, and EXCLUSIVE. The article title is "CBSE Class 12 exam: Issue of tough maths paper raised in Parliament". The sub-headline reads: "A senior Congress member on Thursday raised the issue of the tough mathematics question paper in the ongoing CBSE board examinations and asked the government to consider the issue 'seriously'." The article is dated "Last Updated: Thursday, March 19, 2015 - 14:41". It has 2547 shares (Facebook, Twitter, G+), 16 comments, and 33 comments. A "Follow @ZeeNews" button is visible. The article text begins with "New Delhi: A senior Congress member on Thursday raised the issue of the tough mathematics question paper in the ongoing CBSE board examinations and asked the government to consider the issue 'seriously'."

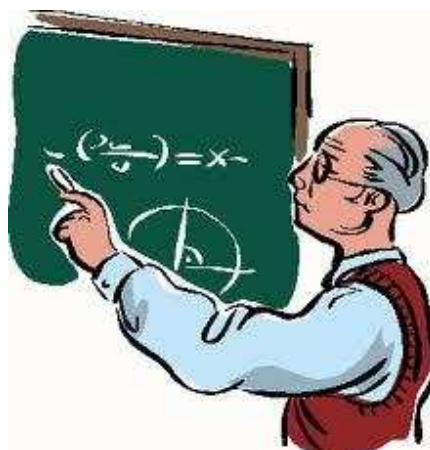
These complains are not new. In fact since last 40 years, ( since my childhood ), I always see this; every year the same setback, same complain!

In this e-Book I am trying to solve this problem. Those students who practice can learn.

**No one can help those who are not studying, or practicing.**

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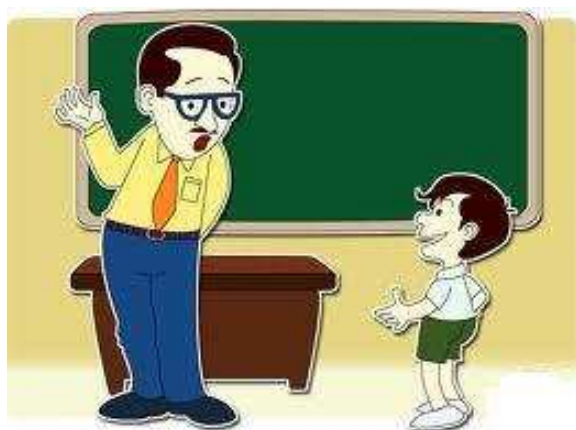
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## Spoon Feeding Series - Differential Equation

In any book solution techniques of various types of Differential equations will be given. But in exam when you get one, you are not sure of what type is it. So you have to try the various methods one by one .....

**The approach to solve Differential Equations would be as follows.**

Step -1 Check if the problem is of type variable separable

If yes then solve it

Else

Step -2 Check if it is of the type exact. This is because it is easiest or fastest to solve differential equations of exact type

Else step -3 Check if the problem is modifiable to “ Exact type “. ( by multiplying with a I.F ( Integrating Factor ) )

If you could identify the multiplying factor and modified then solve it as EXACT type

Else step -4 Check if some differential coefficients can be squeezed ?

Else step -5 check if it is homogeneous type ? ( or is it reducible to homogeneous ) ?

Else step -6 check if it linear or modifiable to linear.

Else step -7 check if it is of the form Bernoulli ( This is also modifiable to linear )

Else step -8 check if it can be written as D parameter and factorized.

But before we proceed with examples and types of Differential Equations, it is important to recall the Integration rules or methods. ( This chapter assumes that the students is very good at Indefinite Integral. )

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IIT-JEE IGCSE Home Tutions South Bangalore by Prof. Subhashish Chattopadhyay and Team of Teachers

<http://iitjeeigcse.simplesite.com/>

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Recall the various tricks, formulae, and rules of solving Indefinite Integrals

$$(i) \int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$(ii) \int \frac{1}{a^2 - x^2} dx = \frac{1}{2a} \log \left| \frac{a+x}{a-x} \right| + C = \frac{1}{a} \tanh^{-1} \left( \frac{x}{a} \right) + C$$

$$(iii) \int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \log \left| \frac{x-a}{x+a} \right| + C = -\frac{1}{a} \coth^{-1} \left( \frac{x}{a} \right) + C$$

$$(iv) \int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C$$

$$(v) \int \frac{dx}{\sqrt{x^2 - a^2}} = \log |x + \sqrt{x^2 - a^2}| + C = \cosh^{-1} \left( \frac{x}{a} \right) + C$$

$$(vi) \int \frac{dx}{\sqrt{x^2 + a^2}} = \log |x + \sqrt{x^2 + a^2}| + C = \sinh^{-1} \left( \frac{x}{a} \right) + C$$

$$(vii) \int \sqrt{x^2 + a^2} dx = \frac{1}{2} \left[ x\sqrt{x^2 + a^2} + a^2 \log |x + \sqrt{x^2 + a^2}| \right] + C$$

$$(viii) \int \sqrt{a^2 - x^2} dx = \frac{1}{2} \left[ x\sqrt{a^2 - x^2} + a^2 \sin^{-1} \left( \frac{x}{a} \right) \right] + C$$

$$(ix) \int \sqrt{x^2 - a^2} dx = \frac{1}{2} \left[ x\sqrt{x^2 - a^2} - a^2 \log |x + \sqrt{x^2 - a^2}| \right] + C$$

$$(x) \int (px + q) \sqrt{ax^2 + bx + c} dx = \frac{p}{2a} \int (2ax + b) \sqrt{ax^2 + bx + c} dx \\ + \left( \frac{q - pb}{2a} \right) \int \sqrt{ax^2 + bx + c} dx$$



- $\int e^x dx = e^x$
- $\int e^{ax} dx = \frac{1}{a} e^{ax}$
- $\int e^{ax} \cos bx dx = \frac{e^{ax}}{a^2+b^2} (a \cos bx + b \sin bx)$
- $\int e^{ax} \sin bx dx = \frac{e^{ax}}{a^2+b^2} (a \sin bx - b \cos bx)$
- $\int a^x dx = \frac{a^x}{\ln a} + c$
- $\int \log x dx = x(\log x - 1) + c$
- $\int \frac{1}{x} dx = \log |x| + c$
- $\int a^x dx = a^x \log x + c$
- $\int \frac{dx}{a^2-x^2} = \frac{1}{2a} \log \frac{a+x}{a-x} + c$
- $\int \frac{dx}{x^2-a^2} = \frac{1}{2a} \log \frac{x-a}{x+a} + c$
- $\int \csc x \cot x dx = -\csc x + c$
- $\int \csc^2 x dx = -\cot x + c$
- $\int \sec x \tan x dx = \sec x + c$
- $\int \sec^2 x dx = \tan x + c$
- $\int \sin x dx = -\cos x + c$
- $\int \cos x dx = \sin x + c$
- $\int (ax+b)^n = \frac{1}{a} \frac{(ax+b)^{n+1}}{n+1} + C, n \neq -1$
- $\int \frac{dx}{(ax+b)} = \frac{1}{a} \log |ax+b| + C$
- $\int e^{ax+b} = \frac{1}{a} e^{ax+b} + C$
- $\int \cos(ax+b) dx = \frac{1}{a} \sin(ax+b) + C$
- $\int \sec^2(ax+b) dx = \frac{1}{a} \tan(ax+b) + C$
- $\int \csc^2(ax+b) dx = \frac{-1}{a} \cot(ax+b) + C$
- $\int \csc(ax+b) \cot(ax+b) dx = \frac{-1}{a} \csc(ax+b) + C$

Some advanced procedures....

$$\int \frac{x^m}{(a+bx)^p} dx$$

$m$  is a + ve integer

Put  $a + bx = z$

$$\int \frac{dx}{x^m (a+bx)^p}$$

where either ( $m$  and  $p$  positive integers) or ( $m$  and  $p$  are fractions, but  $m + p = \text{integers} > 1$ )

Put  $a + bx = zx$

$$\int x^m (a+bx^n)^p dx,$$

where  $m, n, p$  are rationals.

(i)  $p$  is a + ve integer

Apply Binomial theorem to

$$(a + bx^n)^p$$

Put  $x = z^k$  where  $k = \text{common denominator of } m \text{ and } n.$

(iii)  $\frac{m+1}{n}$  is an integer

Put  $(a + bx^n) = z^k$  where  $k = \text{denominator of } p.$

(iv)  $\frac{m+1}{n} + p$  is an integer

Put  $a + bx^n = x^n z^k$   
where  $k = \text{denominator of fraction } p.$

Solve a Simple Problem

$$\begin{aligned} \int \frac{3x+1}{2x^2+x+1} dx &= \int \left( \frac{\frac{3}{4}(4x+1) + \frac{1}{4}}{2x^2+x+1} \right) dx \\ &= \frac{3}{4} \int \left( \frac{4x+1}{2x^2+x+1} \right) dx + \frac{1}{8} \int \frac{dx}{\left(x^2 + \frac{x}{2} + \frac{1}{2}\right)} \\ &= \frac{3}{4} \log(2x^2+x+1) + \frac{1}{2\sqrt{7}} \tan^{-1} \frac{4x+1}{\sqrt{7}} + C \end{aligned}$$

Solve a problem

$$\int \frac{x}{(1-x)^{1/3} - (1-x)^{1/2}} dx \quad \{ \text{The LCM of 2 and 3 is 6} \}$$

Hence, substitute  $1-x = u^6$  Then,  $dx = -6u^5 du$

$$\Rightarrow I = \int \frac{1-u^6}{u^2-u^3} (-6u^5 du) = -6 \int \frac{1-u^6}{1-u} u^3 du$$

$$= -6 \int (1+u+u^2+u^3+u^4+u^5) u^3 du$$

$$= -6 \left( \frac{1}{4}u^4 + \frac{1}{5}u^5 + \frac{1}{6}u^6 + \frac{1}{7}u^7 + \frac{1}{8}u^8 + \frac{1}{9}u^9 \right) + c$$

Solve a Problem

Evaluate  $\int \cos 2x \log(1 + \tan x) dx$ .

**Solution:**

Integrating by parts taking  $\cos 2x$  as the 2nd function, the given integral

$$= \left\{ \log(1 + \tan x) \right\} \frac{\sin 2x}{2} - \int \frac{\sec^2 x}{1 + \tan x} \cdot \frac{\sin 2x}{2} dx$$

$$= \frac{1}{2} \sin 2x \log(1 + \tan x) - \int \frac{\sin x}{\sin x + \cos x} dx.$$

Now  $\int \frac{\sin x dx}{\sin x + \cos x}$

$$= \frac{1}{2} \int \frac{(\sin x + \cos x) - (\cos x - \sin x)}{\sin x + \cos x} dx,$$

$$= \frac{1}{2} \int \left[ 1 - \frac{\cos x - \sin x}{\sin x + \cos x} \right] dx = \frac{1}{2} [x - \log(\sin x + \cos x)].$$

Hence the given integral

$$= \frac{1}{2} \sin 2x \log(1 + \tan x) - \frac{1}{2} [x - \log(\sin x + \cos x)].$$

Recall how to integrate Linear X root Quadratic in denominator

Find the value of the  $\int \frac{dx}{(x+1)\sqrt{(1+2x-x^2)}}$

Putting  $(x+1) = \frac{1}{t}$ , so that  $dx = -\frac{1}{t^2} dt$ ,  $x = \frac{1-t}{t}$  and

$$(1+2x-x^2) = 1 + 2\left(\frac{1-t}{t}\right) - \frac{(1-t)^2}{t^2} = \frac{2}{t^2} \left[ \left(\frac{1}{\sqrt{2}}\right)^2 - (t-1)^2 \right],$$

we get the value of the given **integral** transformed as'

$$\int \frac{-\frac{1}{t^2} dt}{\frac{1}{t} \frac{2}{\sqrt{t}} \left[ \left( \frac{1}{\sqrt{2}} \right)^2 - (t-1)^2 \right]} = -\frac{1}{\sqrt{2}} \sin^{-1} \frac{t-1}{\left( \frac{1}{\sqrt{2}} \right)} + C$$

$$= \frac{1}{\sqrt{2}} \sin^{-1} \frac{\sqrt{2} x}{(x+1)} + C$$

Another advanced example

**Example** Evaluate  $\int \frac{dx}{x\sqrt{1+x^n}}$

Make the substitution  $(1+x^n) = t^2$  or  $x^n = (t^2 - 1)$ , so that  $n x^{n-1} dx = 2t dt$ , we get

$$\int \frac{2t dt}{n x^n t} = \frac{2}{n} \int \frac{dt}{(t^2 - 1)} = \frac{1}{n} \ln \left| \frac{t-1}{t+1} \right|$$

$$= \frac{1}{n} \ln \left| \frac{\sqrt{1+x^n} - 1}{\sqrt{1+x^n} + 1} \right| + C$$

Similarly

The value of integral  $\int \frac{dx}{x\sqrt{1-x^3}}$  is given by

(a)  $\frac{1}{3} \log \left| \frac{\sqrt{1-x^3} + 1}{\sqrt{1-x^3} - 1} \right| + C$       (b)  $\frac{1}{3} \log \left| \frac{\sqrt{1-x^3} - 1}{\sqrt{1-x^3} + 1} \right| + C$

(c)  $\frac{2}{3} \log \left| \frac{1}{\sqrt{1-x^3}} \right| + C$       (d)  $\frac{1}{3} \log |1-x^3| + C$

**Ans. (b)**

**Solution** Put  $1-x^3 = t^2$ . Then  $-3x^2 dx = 2t dt$  and the integral becomes

$$\begin{aligned} -\frac{1}{3} \int \frac{-3x^2 dx}{x^3 \sqrt{1-x^3}} &= -\frac{1}{3} \int \frac{2t dt}{(1-t^2)t} = \frac{2}{3} \int \frac{dt}{t^2-1} \\ &= \frac{2}{3} \left( \frac{1}{2} \log \left| \frac{t-1}{t+1} \right| \right) + C = \frac{1}{3} \log \left| \frac{\sqrt{1-x^3}-1}{\sqrt{1-x^3}+1} \right| + C \end{aligned}$$

Solve a Problem

$\int \sqrt{\sec x - 1} dx$  is equal to

(a)  $2 \log \left( \cos \frac{x}{2} + \sqrt{\cos^2 \frac{x}{2} - \frac{1}{2}} \right) + C$

(b)  $\log \left( \cos \frac{x}{2} + \sqrt{\cos^2 \frac{x}{2} - \frac{1}{2}} \right) + C$

(c)  $-2 \log \left( \cos \frac{x}{2} + \sqrt{\cos^2 \frac{x}{2} - \frac{1}{2}} \right) + C$

(d) none of these

$$\begin{aligned} \text{(c). } \int \sqrt{\sec x - 1} \, dx &= \int \sqrt{\frac{1 - \cos x}{\cos x}} \, dx \\ &= \sqrt{2} \int \frac{\sin \frac{x}{2}}{\sqrt{2 \cos^2 \frac{x}{2} - 1}} \, dx = -2 \sqrt{2} \int \frac{dz}{\sqrt{2z^2 - 1}} \\ &\quad \left( \text{Putting } \cos \frac{x}{2} = z \Rightarrow \sin \frac{x}{2} \, dx = -2dz \right) \\ &= -2 \int \frac{dz}{\sqrt{z^2 - \left(\frac{1}{\sqrt{2}}\right)^2}} \\ &= -2 \log \left[ z + \sqrt{z^2 - \left(\frac{1}{\sqrt{2}}\right)^2} \right] + C \\ &= -2 \log \left( \cos \frac{x}{2} + \sqrt{\cos^2 \frac{x}{2} - \frac{1}{2}} \right) + C \end{aligned}$$

Solve another problem

$$\begin{aligned}
 I &= \int \sqrt{1 + \operatorname{cosec} x} \cdot dx \\
 &= \int \sqrt{1 + \frac{1}{\sin x}} \cdot dx = \int \sqrt{\frac{\sin x + 1}{\sin x}} \cdot dx \\
 &= \int \sqrt{\frac{(1 + \sin x)(1 - \sin x)}{\sin x(1 - \sin x)}} \cdot dx && \text{[On rationalization]} \\
 &= \int \sqrt{\frac{1 - \sin^2 x}{\sin x - \sin^2 x}} \cdot dx && [\because (a + b)(a - b) = a^2 - b^2] \\
 &= \int \frac{\cos x}{\sqrt{\sin x - \sin^2 x}} \cdot dx && [\because \sin^2 A + \cos^2 A = 1] \\
 \sin x = z &\Rightarrow \cos x \, dx = dz \\
 I &= \int \frac{1}{\sqrt{z - z^2}} \cdot dz = \int \frac{1}{\sqrt{-(z^2 - z)}} \cdot dz \\
 &= \int \frac{1}{\sqrt{\frac{1}{4} - \left(z^2 - z + \frac{1}{4}\right)}} \cdot dz && \left[ \begin{array}{l} \text{Add and subtract } \frac{1}{4} \text{ to the denom.} \\ \because \left(\frac{1}{2} \text{ coeff. of } x\right)^2 = \frac{1}{4} \end{array} \right] \\
 &= \int \frac{1}{\sqrt{\left(\frac{1}{2}\right)^2 - \left(z - \frac{1}{2}\right)^2}} \cdot dz \\
 \left(z - \frac{1}{2}\right) &= y \Rightarrow dz = dy \\
 I &= \int \frac{1}{\sqrt{\left(\frac{1}{2}\right)^2 - y^2}} \cdot dy && \left[ \text{By using } \int \frac{1}{\sqrt{a^2 - x^2}} \cdot dx = \sin^{-1}\left(\frac{x}{a}\right) + c \right] \\
 &= \sin^{-1}\left(\frac{y}{1/2}\right) + c \\
 &= \sin^{-1}\left(\frac{z - 1/2}{1/2}\right) + c && [\because y = z - 1/2]
 \end{aligned}$$



Solve another Integral

$$\begin{aligned}
 I &= \int \sqrt{\frac{1+x}{x}} \cdot dx \\
 &= \int \sqrt{\frac{1+x}{x} \times \frac{1+x}{1+x}} dx && \text{[Multiply and divided by } (1+x)\text{]} \\
 &= \int \sqrt{\frac{(1+x)^2}{x(1+x)}} \cdot dx = \int \frac{1+x}{\sqrt{x+x^2}} \cdot dx
 \end{aligned}$$

Let us write :

$$\begin{aligned}
 1+x &= \lambda \cdot \frac{d}{dx} (x+x^2) + \mu \\
 \Rightarrow 1+x &= \lambda (1+2x) + \mu && \dots(1) \\
 \Rightarrow 1+x &= 2\lambda x + \lambda + \mu
 \end{aligned}$$

Comparing the coefficients of  $x$  and the constant terms, we have

$$1 = 2\lambda \Rightarrow \lambda = \frac{1}{2}$$

and

$$1 = \lambda + \mu \Rightarrow \mu = 1 - \lambda = 1 - \frac{1}{2} = \frac{1}{2}$$

Putting the values of  $\lambda$  and  $\mu$  in (1),

$$1+x = \frac{1}{2} (1+2x) + \frac{1}{2}$$

$$\begin{aligned}
 \therefore I &= \int \frac{\frac{1}{2} (1+2x) + \frac{1}{2}}{\sqrt{x+x^2}} \cdot dx \\
 &= \frac{1}{2} \int \frac{1+2x}{\sqrt{x+x^2}} dx + \frac{1}{2} \int \frac{1}{\sqrt{x+x^2}} \cdot dx
 \end{aligned}$$

$$\Rightarrow I = \frac{1}{2} I_1 + \frac{1}{2} I_2 \quad \dots(2)$$

Now  $I_1 = \int \frac{1+2x}{\sqrt{x+x^2}} dx$

Put  $x+x^2 = z \Rightarrow (1+2x) dx = dz$

$$\begin{aligned}
 \therefore I_1 &= \int \frac{1}{\sqrt{z}} \cdot dz = \int z^{-1/2} \cdot dz = \frac{z^{-\frac{1}{2}+1}}{-\frac{1}{2}+1} + c_1 = 2\sqrt{z} + c_1 \\
 &= 2\sqrt{x+x^2} + c_1 && \dots(3)
 \end{aligned}$$

and

$$I_2 = \int \frac{1}{\sqrt{x+x^2}} \cdot dx$$

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