

Adaptive Beamforming Algorithm Using a Pre-filtering System

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1. Introduction

As depicted in Fig. 1, adaptive beamforming algorithms can be classified into two categories: non-blind adaptive algorithms and blind adaptive algorithms [1]. Non-blind adaptive algorithms rely on statistical knowledge about the transmitted signal in order to converge to a solution. This is typically accomplished through the use of a pilot training sequence sent over the channel to the receiver to help it identifying the desired user. On the other hand, blind adaptive algorithms do not require prior training, and hence they are referred to as "blind" algorithms. These algorithms attempt to extract salient characteristic of the transmitted signal in order to separate it from other users in the surrounding environment [2]. In this chapter we propose a technique that could be used with the blind or non blind algorithms to enhance their performance. This technique acts on the input signal vector $\mathbf{x}(k)$ as a band pass filter but in spatial domain, so it minimizes the noise and interference effects as a function of the Direction of Arrivals (DOAs).

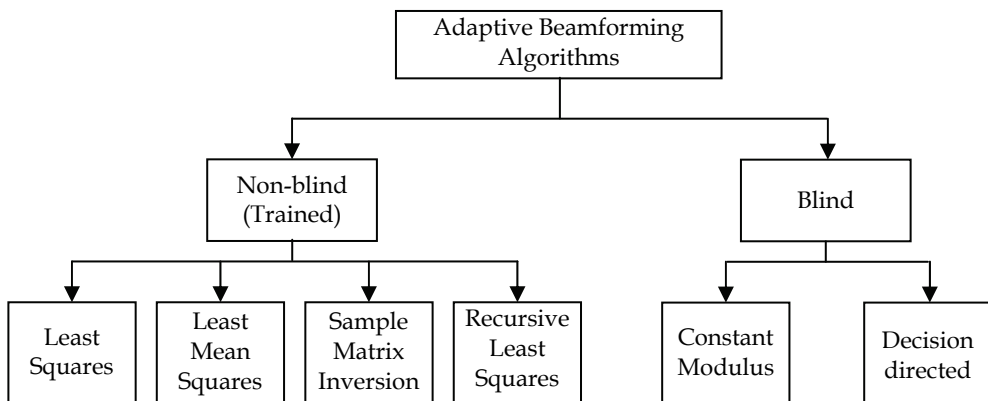


Fig. 1. General classifications of adaptive array algorithms

Source: Aerospace Technologies Advancements, Book edited by: Dr. Thawar T. Arif, ISBN 978-953-7619-96-1, pp. 492, January 2010, INTECH, Croatia, downloaded from SCIYO.COM

2. Proposed hybrid adaptive beamforming technique

The proposed technique which introduced in [3] aims to increase the Signal-to-Interference and Noise Ratio (SINR) of the beamforming system by reducing the interference and noise effects on the desired user signal using filtering in spatial domain, or extracting the desired signal from the instantaneous input signal vector $\mathbf{x}(k)$ of the beamformer, as can be seen in Fig. 2. In this context, it is worth pointing out that in image processing, especially in image compressing techniques, one can find an abundance of techniques that can reconstruct the original image with acceptable performance, without using all transformation components, but rather using only the lower component coefficients of the image transform matrix [4]. We will exploit this fact with some modifications and employ it in the antenna array processing to obtain a new beamforming technique.

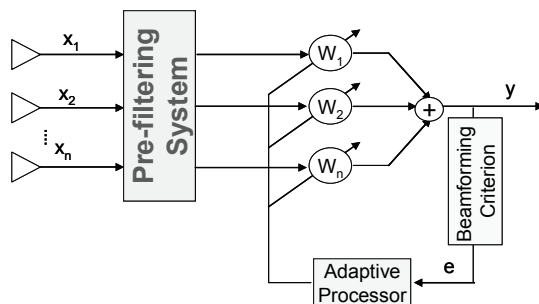


Fig. 2. Proposed blind adaptive beamformer with pre-filtering system

Since the interfering signals are in the same frequency band of the desired signal, we investigate representing them in another domain other than frequency domain so as to distinguish between the mixed signals that form the input signal. Therefore, the proposed technique is based on the idea that the desired and interfering signals arrive at the antenna array from different directions. Thus, we exploit these differences between arriving signals. The distinction can be obtained by converting the input signal to the spectrum of the spatial domain (this domain is the sine of the direction of arrival, or $\sin\theta$ domain). The desired signal can be extracted from the input system signals simply by making a band-pass filter in the spectrum of the spatial domain, i.e., in the $\sin\theta$ spectrum. This filtering process is shown in Fig. 3, and can be explained generally as follows:

- The original input signal is passed through a Fast Fourier Transform (FFT) stage to obtain its coefficients in the spectrum domain.
- The Most Significant Coefficient (MSC) of the transformed signal is selected. This is ranked as the largest sample of the transformed desired signal.
- The most significant coefficient is placed at its rank in the M zeros element vector (zero padding).
- The Inverse Fast Fourier Transform (IFFT) is applied to the filtered vector of the previous step to reconstruct an alternative input signal that contains a reduced amount of interference and noise.
- The reconstructed data vector is used as input signal to the adaptive beamforming system.

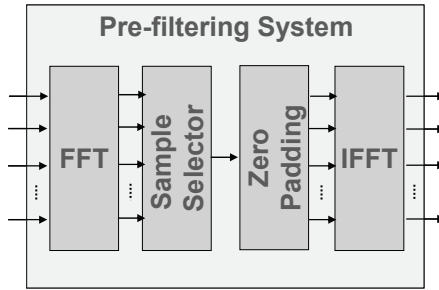


Fig. 3. Pre-filtering system

Mathematically, assuming that the narrow band array propagation vector for the θ direction of arrival is given by

$$\mathbf{a}(\theta) = e^{-j2\pi\frac{d}{\lambda}\sin\theta(m-1)}, \quad m = 1, 2, \dots, M \tag{1}$$

where M is the number of array elements, d is the spacing distance between any two adjacent elements, and λ is the wavelength of the operating carrier frequency. Applying the FFT on the array propagation (Equation 1) gives

$$\begin{aligned} \mathbf{A}(\Theta) &= FFT(\mathbf{a}(\theta)) \\ &= \frac{1}{M} \sum_{m=1}^M e^{-j2\pi\frac{d}{\lambda}\sin\theta(m-1)} e^{-j2\pi K(m-1)/M} \\ &= \frac{1}{M} \sum_{m=1}^M e^{-j2\pi\left(\frac{d}{\lambda}\sin\theta(m-1) + \frac{K}{M}(m-1)\right)} \end{aligned} \tag{2}$$

Let $d = \lambda/2$, then

$$\begin{aligned} \mathbf{A}(\Theta) &= \frac{1}{M} \sum_{m=1}^M e^{-j2\pi\left(\frac{K}{M} + \frac{\sin\theta}{2}\right)(m-1)} \\ &= \frac{1}{M} \frac{e^{j\pi(2K+M\sin\theta)/M} - e^{-j2\pi(2K+M\sin\theta)(M-1)/M}}{e^{j\pi(2K+M\sin\theta)/M} - 1} \\ &= \frac{1}{M} \left[\frac{e^{j\pi\left(\frac{2K+\sin\theta}{M}\right)\left(\frac{3-2M}{2}\right)} \left[e^{j\pi\left(\frac{2K+M\sin\theta}{M}\right)\left(M-\frac{1}{2}\right)} - e^{-j\pi\left(\frac{2K+M\sin\theta}{M}\right)\left(M-\frac{1}{2}\right)} \right]}{e^{j\pi\left(\frac{2K+\sin\theta}{2M}\right)} \left[e^{j\pi\left(\frac{2K+M\sin\theta}{2M}\right)} - e^{-j\pi\left(\frac{2K+M\sin\theta}{2M}\right)} \right]} \right] \\ &= e^{-j\pi\left(\frac{2K+\sin\theta}{M}\right)(M-1)} \left[\frac{\sin\left(\pi\left(\frac{2K+M\sin\theta}{M}\right)\left(M-\frac{1}{2}\right)\right)}{M \sin\left(\pi\left(\frac{2K+M\sin\theta}{2M}\right)\right)} \right] \end{aligned} \tag{3}$$

By differentiating Equation (3) and equating the result to zero, the following formula gives the index K_{MSC} (or the order) of the most significant coefficient as a function of the direction of arrival θ and the number of array elements M

$$K_{MSC} = \left[-\frac{1}{2} \left[\frac{M \left[2\pi M \sin \theta - \pi \sin \theta + j 2 \tanh^{-1} \left(\frac{M - \frac{1}{2}}{M - 1} \right) \right]}{\pi(2M - 1)} \right] \right]_{\text{int}} \quad (4)$$

where $[x]_{\text{int}}$ means the integer part of x .

Since the index K_{MSC} must be a real integer, the formula in Equation (4) is modified to take the form

$$K_{MSC} = \text{mod}_M \left\{ 1 + M \left[-\frac{1}{2} \left(\frac{M(2\pi M \sin \theta - \pi \sin \theta)}{\pi(2M - 1)} \right) \right]_{\text{int}} \right\} \quad (5)$$

where mod_M is the modulus notation, performed on M points.

Equation (5) can be simplified to

$$K_{MSC} = \text{mod}_M \left(\left[1 - \frac{1}{2} M \sin \theta \right] \right) \quad (6)$$

To illustrate the idea of the pre-filtering system consider, as an example, an array of 4 elements, with desired DOA = -45° and signal sample $s_d = -0.0035 - 0.1000i$. Then, from Equation (1) the array propagation factor at the desired direction is

$$\mathbf{a}(\theta_d) = \begin{bmatrix} 0.9990 - 0.0000i \\ -0.6049 + 0.7958i \\ -0.2663 - 0.9623i \\ 0.9280 + 0.3715i \end{bmatrix}$$

Thus, the desired signal vector $\mathbf{s} = s_d \mathbf{a}(\theta_d)$ is given by

$$\mathbf{s} = \begin{bmatrix} -0.0035 - 0.0999i \\ 0.0817 + 0.0577i \\ -0.0953 + 0.0300i \\ 0.0339 - 0.0941i \end{bmatrix}$$

And assuming that there is an undesired signal vector \mathbf{u} , such that:

$$\mathbf{u} = \begin{bmatrix} -0.0241 - 0.7054i \\ -0.7078 + 0.0253i \\ 0.0239 + 0.7065i \\ 0.7069 - 0.0256i \end{bmatrix}$$

Thus, by adding the weighted desired and the desired signals the total input signal is given as:

$$\mathbf{x} = \begin{bmatrix} -0.0276 - 0.8053i \\ -0.6261 + 0.0830i \\ -0.0714 + 0.7365i \\ 0.7408 - 0.1197i \end{bmatrix}$$

By passing this input data vector through the FFT stage, we get the following transform coefficients vector

$$\mathbf{X} = \begin{bmatrix} 0.0156 - 0.1055i \\ 0.2465 - 0.1749i \\ -0.2137 - 0.0322i \\ -0.1589 - 2.9087i \end{bmatrix}$$

Applying Equation (6) on the given DOA and the number of array elements we find that the most significant coefficient is the second coefficient. Replacing the other coefficients by zeros, we get the following vector

$$\mathbf{X}_z = \begin{bmatrix} 0 \\ 0.2465 - 0.1749i \\ 0 \\ 0 \end{bmatrix}$$

Now, applying the IFFT on the zero padded vector we get the reconstructed input vector as follows

$$\tilde{\mathbf{x}} = \begin{bmatrix} 0.0616 - 0.0437i \\ 0.0437 + 0.0616i \\ -0.0616 + 0.0437i \\ -0.0437 - 0.0616i \end{bmatrix}$$

To take advantage of the pre-filtering technique to reduce the mean square error (MSE), we determine the fluctuations of the original input data vector $\tilde{\mathbf{x}}$ and the reconstructed input data vector \mathbf{x} from the desired signal vector \mathbf{s}

$$\mathbf{s} - \mathbf{x} = \begin{bmatrix} 0.0241 + 0.7054i \\ 0.7078 - 0.0253i \\ -0.0239 - 0.7065i \\ -0.7069 + 0.0256i \end{bmatrix}$$

$$\mathbf{s} - \tilde{\mathbf{x}} = \begin{bmatrix} -0.0652 - 0.0562i \\ 0.0379 - 0.0039i \\ -0.0338 - 0.0137i \\ 0.0776 - 0.0324i \end{bmatrix}$$

MSE of the conventional technique = $20 \log(|s - \mathbf{x}|) = 9.0306 \text{ dBv}$

MSE of the proposed technique = $20 \log(|s - \tilde{\mathbf{x}}|) = -12.2258 \text{ dBv}$.

It is clear that the proposed technique reduces the MSE in this example by more than 21 dB; this improvement is significant in communications systems.

As explained in the general steps shown in Fig. 4, the output of the pre-filtering stage is applied as an input to the beamforming algorithms. The flowchart of the whole process using the constant modulus algorithm CMA(1,2) is as indicated in the figure. Other algorithms (other than the CMA) can also be used.

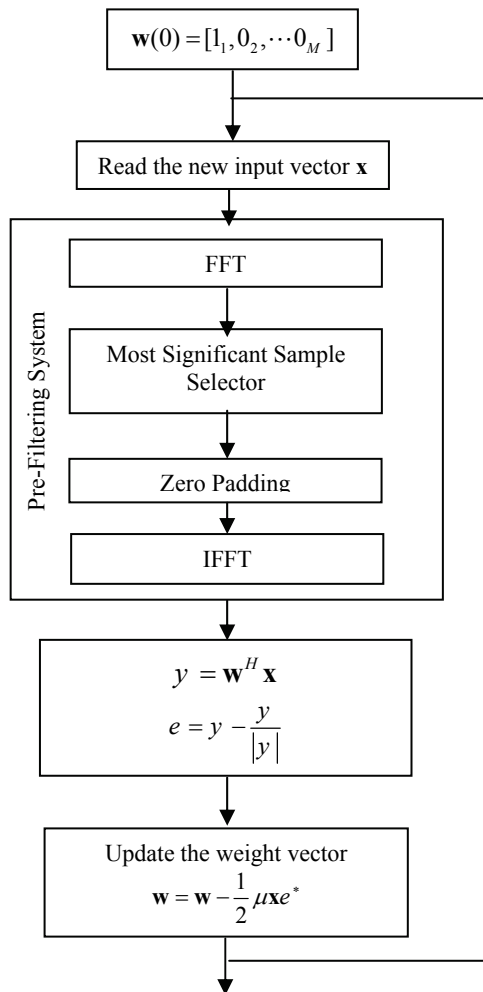


Fig. 4. Flowchart of the proposed hybrid technique

3. Quadratic diagram and the SIR improvement in the beamformer input signal using the proposed hybrid technique

The quadratic (i.e. the complex plane) diagram of the input signal vector to the beamformer system is represented in Fig.5, where s_i, u_i and x_i represent, respectively, the desired, undesired and the total input signal on the i th element of the array. For clarity, only the angles of s_1, u_1, x_1 are shown.

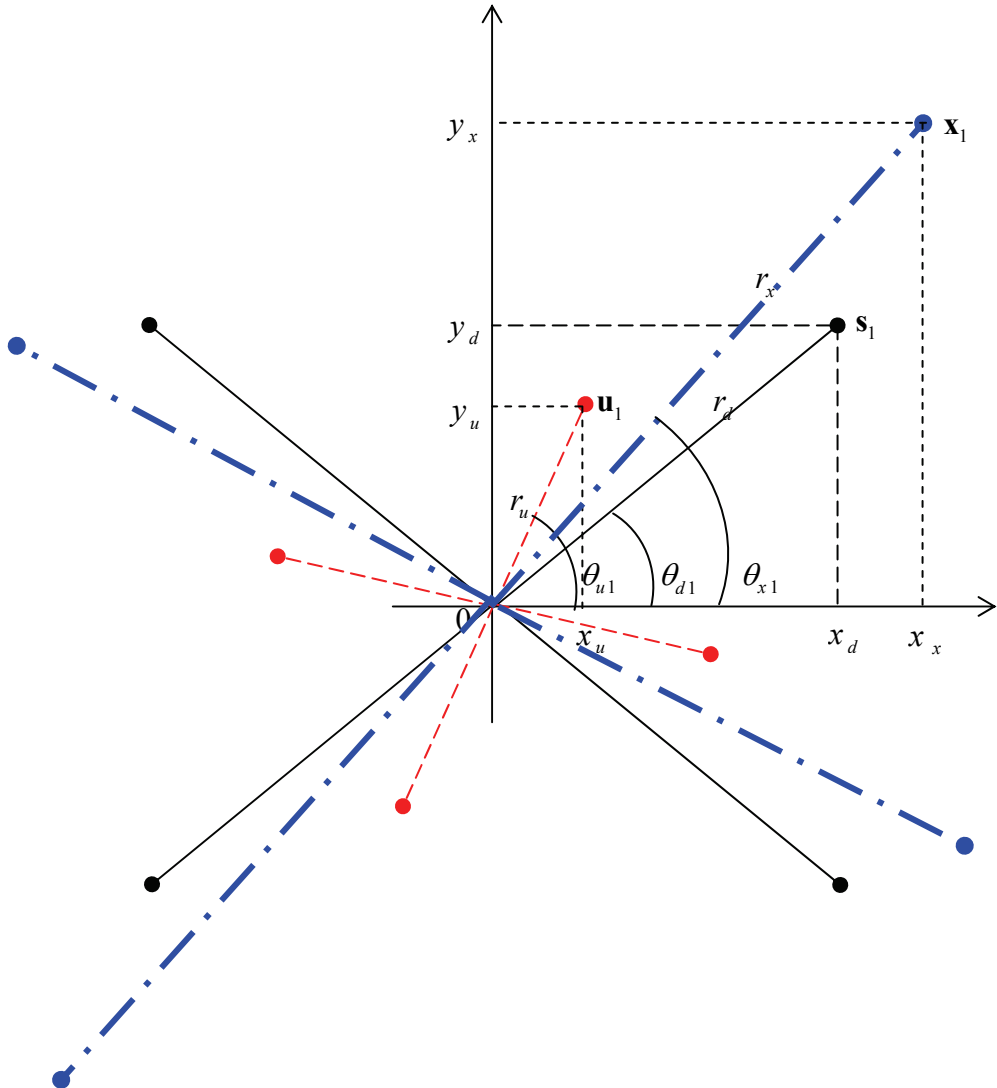


Fig. 5. The desired, interfering and the total input signal vectors in the quadratic plane
The desired signal vector can be represented as

$$\mathbf{s} = s\mathbf{a}(\theta_d) \quad (7)$$

where $\mathbf{a}(\theta_d)$ is the array propagation vector corresponding to the desired direction and it is given as,

$$\mathbf{a}(\theta_d) = e^{-j\frac{2\pi}{\lambda}(m-1)d \sin \theta_d}, m = 1, 2, \dots, M$$

and $s = r_d e^{j\phi_d}$ is the desired signal sample. Equation (7) can be put in the form

$$\mathbf{s} = r_d e^{j\phi_d} e^{-j\frac{2\pi}{\lambda}(m-1)d \sin \theta_d} \quad (8)$$

Assuming $d = \lambda/2$, the desired signal vector can be written in the form

$$\mathbf{s} = r_d e^{j(\phi_d - \pi(m-1)\sin \theta_d)} \quad (9)$$

The complex rectangular coordinates of the vectors can be expressed as

$$x_d = r_d \cos(\phi_d - \pi(m-1)\sin \theta_d) \quad (10a)$$

$$y_d = r_d \sin(\phi_d - \pi(m-1)\sin \theta_d) \quad m = 1, 2, \dots, M \quad (10b)$$

It is clear that the resulting signal is an array containing vectors with a constant magnitude r_d , and each vector has a specific phase $\phi_d(m) = -\pi(m-1)\sin \theta_d$, $m = 1, 2, \dots, M$. Similarly, the undesirable signal vector can be put in the form

$$\mathbf{u} = r_u e^{j(\phi_u - \pi(m-1)\sin \theta_u)} \quad (11)$$

the complex rectangular coordinates of which can be expressed as

$$x_u = r_u \cos(\phi_u - \pi(m-1)\sin \theta_u)$$

$$y_u = r_u \sin(\phi_u - \pi(m-1)\sin \theta_u) \quad (12)$$

In case of interference, the total received signal can be put as

$$\mathbf{x} = \mathbf{s} + \mathbf{u} \quad (13)$$

$$\mathbf{x} = r_d e^{j(\phi_d - \pi(m-1)\sin \theta_d)} + r_u e^{j(\phi_u - \pi(m-1)\sin \theta_u)} \quad (14)$$

for which, the complex rectangular coordinates may be written as:

$$x_x = r_d \cos(\phi_d - \pi(m-1)\sin \theta_d) + r_u \cos(\phi_u - \pi(m-1)\sin \theta_u)$$

$$y_x = r_d \sin(\phi_d - \pi(m-1)\sin \theta_d) + r_u \sin(\phi_u - \pi(m-1)\sin \theta_u) \quad (15)$$

The resulting overall vector magnitude can be obtained as follows

$$\begin{aligned}
 r_x &= \sqrt{x_x^2 + y_x^2} \\
 &= \sqrt{(x_d + x_u)^2 + (y_d + y_u)^2} \\
 &= \sqrt{(x_d^2 + y_d^2) + (x_u^2 + y_u^2) + 2(x_d x_u + y_d y_u)} \\
 &= \sqrt{(r_d^2 + r_u^2) + 2r_d r_u \psi}
 \end{aligned} \tag{16}$$

where

$$\begin{aligned}
 \psi &= \cos(\phi_d - \pi(m-1)\sin\theta_d)\cos(\phi_u - \pi(m-1)\sin\theta_u) \\
 &\quad + \sin(\phi_d - \pi(m-1)\sin\theta_d)\sin(\phi_u - \pi(m-1)\sin\theta_u)
 \end{aligned} \tag{17}$$

is the variation in the total signal magnitude (desired and undesired signals) caused by the interference (undesirable signals). Here, $\psi(m)$ is not a constant value for all values of m except when θ_d and θ_u are equal; in this case the proposed technique will not improve SIR; but generally most of beamforming algorithms fail in this case. Since we have assumed in this chapter that the interfering signal arrive at a direction different from the desired signal direction, $r_x(m)$ can not to be a constant value, i.e., the total input signal vector $\mathbf{x}(m)$ will appear scattered in the complex plane.

To show the Signal-to-Interference Ratio (SIR) improvement in the input signal vector using the proposed hybrid beamforming technique we determine the gained signal-to-interference ratio in the reconstructed signal vector using the pre-filtering technique of the hybrid beamforming system. Assuming a linear system, the total input signal vector $x(m)$ is the sum of the desired signal $\mathbf{s}(m)$ and the undesired one $\mathbf{u}(m)$ -i.e.-

$$\mathbf{x}(m) = \mathbf{s}(m) + \mathbf{u}(m) \tag{18}$$

Similarly, for the reconstructed input data vector $\tilde{\mathbf{x}}(m)$,

$$\tilde{\mathbf{x}}(m) = \tilde{\mathbf{s}}(m) + \tilde{\mathbf{u}}(m) \tag{19}$$

where $\tilde{\mathbf{s}}(m)$, and $\tilde{\mathbf{u}}(m)$ are the desired and undesired reconstructed signals vector respectively. To generalize the procedure, we will assume that an arbitrary signal sample $v = re^{j\phi}$ arrives to the array at θ direction. Therefore, the array signal vector of this signal will be in the form

$$\mathbf{v}(m) = re^{j\phi} e^{-j\pi \sin\theta(m-1)}, \quad m = 1, 2, \dots, M \tag{20}$$

The fast Fourier transform of the resulting signal vector $\mathbf{v}(m)$ is

$$\begin{aligned}
 \mathbf{V}(k) &= FFT[\mathbf{v}(m)] \\
 &= \sum_{m=1}^M \mathbf{v}(m) \cdot e^{j2\pi(k-1)(m-1)/M} \\
 &= \sum_{m=1}^M re^{j\phi} \cdot e^{j2\pi(k-1)(m-1)/M}
 \end{aligned}$$

$$\begin{aligned}
 &= re^{j\phi} \cdot e^{-j\frac{\pi}{2}[M \sin \theta + 2(k-1)](M+1)/M} \\
 &\cdot \left[\frac{\sin\left(\frac{\pi}{2}[M \sin \theta + 2(k-1)]\right)}{\sin\left(\frac{\pi}{2}[M \sin \theta + 2(k-1)]/M\right)} \right] \quad (21)
 \end{aligned}$$

Now, the value of the specific k th coefficient from the transformed signal vector $\mathbf{V}(k)$ can be calculated. This coefficient will be selected to reconstruct the signal vector $\tilde{\mathbf{v}}(m)$. Substituting for the k th index in Equation (6) into Equation (21) gives the value of the most significant coefficient as

$$\begin{aligned}
 \mathbf{V}(k_{MSC}) &= re^{j\phi} \cdot e^{-j\frac{\pi M}{2}[\sin \theta - \sin \theta_d](M+1)/M} \\
 &\cdot \left[\frac{\sin\left(\frac{-\pi M}{2}[\sin \theta - \sin \theta_d]\right)}{\sin\left(\frac{\pi}{2}[\sin \theta - \sin \theta_d]\right)} \right] \quad (22)
 \end{aligned}$$

This value will be put in a zeros vector in the rank of the k_{MSC} so that we can express the resulting signal vector as

$$\begin{aligned}
 \mathbf{V}(k_{MSC}) &= re^{j\phi} \cdot e^{-j\frac{\pi M}{2}[\sin \theta - \sin \theta_d](M+1)/M} \\
 &\cdot \left[\frac{\sin\left(\frac{-\pi M}{2}[\sin \theta - \sin \theta_d]\right)}{\sin\left(\frac{\pi}{2}[\sin \theta - \sin \theta_d]\right)} \right] \cdot \delta(k - k_{MSC}), \quad (23) \\
 &k = 1, 2, \dots, M
 \end{aligned}$$

where

$$\delta(k - k_{MSC}) = \begin{cases} 1, & k = k_{MSC} \\ 0, & \text{elsewhere} \end{cases}$$

The reconstructed signal vector can be obtained by applying inverse Fourier transformation to Equation (23) as follows

$$\begin{aligned}
 \tilde{\mathbf{v}}(m) &= \frac{1}{M} \sum_{k=1}^M \mathbf{V}(k_{MSC}) e^{j2\pi(k-1)(m-1)/M} \\
 &= \frac{1}{M} \mathbf{V}(k_{MSC}) e^{-j\pi \sin \theta_d (m-1)} \\
 &= re^{j\phi} e^{-j\pi \sin \theta_d (m-1)} e^{-j\frac{\pi M}{2}[\sin \theta - \sin \theta_d](M+1)/M} \quad (24a) \\
 &\cdot \left[\frac{\sin\left(\frac{-\pi M}{2}[\sin \theta - \sin \theta_d]\right)}{\sin\left(\frac{\pi}{2}[\sin \theta - \sin \theta_d]\right)} \right]
 \end{aligned}$$

Therefore, we can put the signals in the form

$$\tilde{\mathbf{v}} = G_1(r, \phi, \theta) \cdot G_2(\theta) \tag{24b}$$

where

$$G_1(r, \phi, \theta) = r e^{j\phi} \cdot e^{-j\pi \sin \theta_d (m-1)} \cdot e^{-j\frac{\pi M}{2} [\sin \theta - \sin \theta_d] (M+1)/M} \tag{24c}$$

It is clear from Equation (24 c) that the magnitude of G_1 equals the signal magnitude r and

$$G_2(\theta) = \frac{1}{M} \left[\frac{\sin\left(\frac{-\pi M}{2} [\sin \theta - \sin \theta_d]\right)}{\sin\left(\frac{\pi}{2} [\sin \theta - \sin \theta_d]\right)} \right] \tag{24d}$$

The variation of G_2 as a function of θ is shown in Fig. 6 from which it is clear that its value equal unit only if and only $\theta = \theta_d$. Fig. 7 shows the effects of the gains on the magnitude of the desired, undesired and the total input signal.

In Fig. 7, it is assumed that $r_d > r_u$ without loss of generality.

Note that, in case of $\tilde{\mathbf{s}}$

$$G_1(r_d, \phi_d, \theta_d) = r_d e^{j\phi_d} e^{-j\pi \sin \theta_d (m-1)} \tag{25a}$$

and from Equation (2d)

$$G_2(\theta_d) = 1 \tag{25b}$$

Note that, in case of $\tilde{\mathbf{u}}$

$$G_1(r_u, \phi_u, \theta_u) = r_u e^{j\phi_u} \cdot e^{-j\pi \sin \theta_d (m-1)} \cdot e^{-j\frac{\pi M}{2} [\sin \theta_u - \sin \theta_d] (M+1)/M} \tag{25c}$$

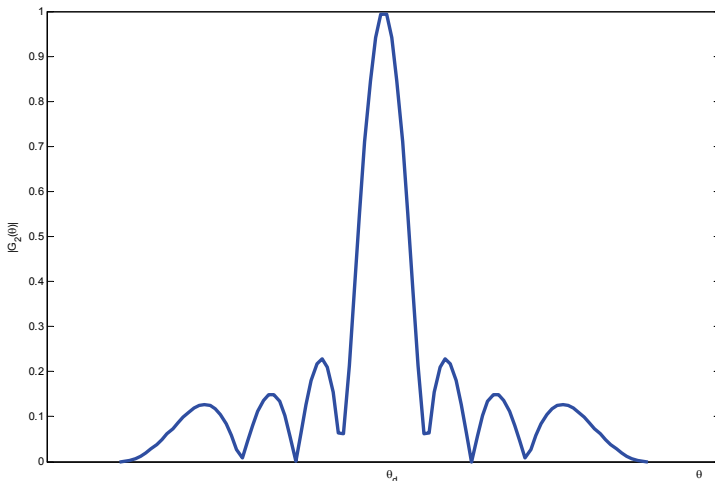


Fig. 6. Magnitude of G_2 versus DOA

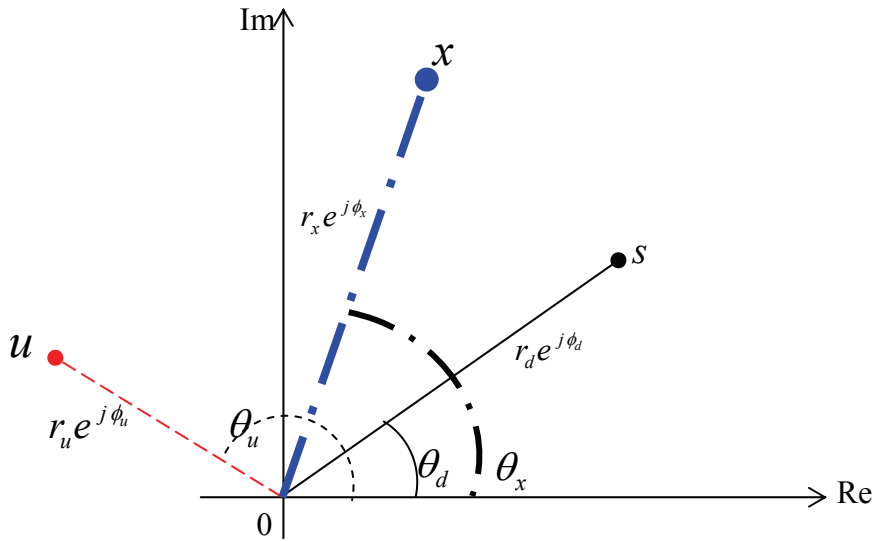


Fig. 7. Desired, interference and the total input signal in the quadratic plane and

$$G_2(\theta_u) = \frac{1}{M} \left[\frac{\sin\left(\frac{-\pi M}{2} [\sin \theta_u - \sin \theta_d]\right)}{\sin\left(\frac{\pi}{2} [\sin \theta_u - \sin \theta_d]\right)} \right] \tag{25d}$$

Note that in case of the desired signal (i.e. $\theta = \theta_d$) G_2 will be equals one i.e. the maximum value. However, in case of the undesired signal (i.e. $\theta = \theta_u$) G_2 will be attenuated i.e. will be less than one.

The overall reconstructed input signal vector $\tilde{\mathbf{x}}(m)$, which consists of the desired signal vector and attenuated interfering signal vector can be given by

$$\tilde{\mathbf{s}} = G_1(r_d, \phi_d, \theta_d) \cdot G_2(\theta_d)$$

and

$$\tilde{\mathbf{u}} = G_1(r_u, \phi_u, \theta_u) \cdot G_2(\theta_u) \tag{26}$$

Substituting Equation (26) into Equation (19) gives

$$\begin{aligned} \tilde{\mathbf{x}}(m) &= r_d e^{j\phi_d} e^{-j\pi \sin \theta_d (m-1)} \\ &+ r_u e^{j\phi_u} e^{-j\pi \sin \theta_d (m-1)} e^{-j\frac{\pi M}{2} [\sin \theta_u - \sin \theta_d] (M+1)/M} \\ &\cdot \frac{1}{M} \left[\frac{\sin\left(\frac{-\pi M}{2} [\sin \theta_u - \sin \theta_d]\right)}{\sin\left(\frac{\pi}{2} [\sin \theta_u - \sin \theta_d]\right)} \right] \end{aligned} \tag{27}$$

Note that the overall reconstructed $\tilde{\mathbf{x}}(m)$ (overall reconstructed signal on the m th element) has a constant magnitude, because its derivative with respect to m is zero (i.e. $\frac{d}{dm}(|\tilde{\mathbf{x}}(m)|) = 0$), which means that the hybrid technique eliminates the magnitude fluctuation which is described in Equations (16) and (17).

As a result, we can evaluate the signal-to-interference ratio SIR improvement in the reconstructed input vector $\tilde{\mathbf{x}}(m)$. Since the magnitude of the desired signal vector stays constant without any attenuation and the interfering signal vector magnitude is decreased by the factor $\left| \frac{1}{M} \left[\frac{\sin(-\pi M/2[\sin \theta_u - \sin \theta_d])}{\sin(\pi/2[\sin \theta_u - \sin \theta_d])} \right] \right|$, therefore, the maximum possible gained SIR_G in dB can be expressed as

$$SIR_G = 20 \log \left\{ \left| \frac{M \sin\left(\frac{\pi}{2}[\sin \theta_u - \sin \theta_d]\right)}{\sin\left(\frac{-\pi M}{2}[\sin \theta_u - \sin \theta_d]\right)} \right| \right\} \text{ dB} \quad (28)$$

A simulation setup will be used to show the improvements in the reconstructed input signal vector. Fig. 8 shows a quadratic diagram representation of a desired signal, arriving at DOA of 60° , an interfering signal with arbitrary DOA of 40° , the original received signal without using the pre-filtering technique, and the reconstructed signal after the pre-filtering process. From these results, one can observe that the reconstructed input data vector is closer to the desired signal than the original received input vector which is scattered by the interference effects. For this reason, the pre-filtering process is performed directly before the beamforming process in the proposed hybrid algorithm. This will help the beamformer in extracting the desired signal in easier and faster way.

Fig. 9 illustrates the quadratic diagram of a similar scenario but with the desired signal arriving at DOA of 45° and 6 undesired signals arriving at DOAs of ($19^\circ, 60^\circ, 120^\circ, 240^\circ, 300^\circ, 341^\circ$) with respect to the DOA of the desired signal. In this figure, one can observe the extensively scattering of the compound interfering signal which causes the scattering of the original input data vector. However, the same figure shows that the reconstructed input signal is not scattered and nearer to the desired signal. Thus, pre-filtering effectively reduces the noise and interfering.

In summary, the pre-filtering technique generates a new input data signal with lower undesired signal than the original one. This reduction is obtained previously by taking the most significant coefficient of the desired signal (and ignoring the other coefficients) (similar to bandpass filtering). To see the possibility of reducing the undesired signal by discarding the most significant coefficient of the undesired signal (similar to band reject filtering), the same scenario is used in Fig. 8 gave the results shown in Fig. 10 which illustrates lower performance.

4. Simulation results

This section compares the performance of the proposed hybrid adaptive algorithms with some of conventional adaptive beamforming algorithms. The factors used for this comparison are:

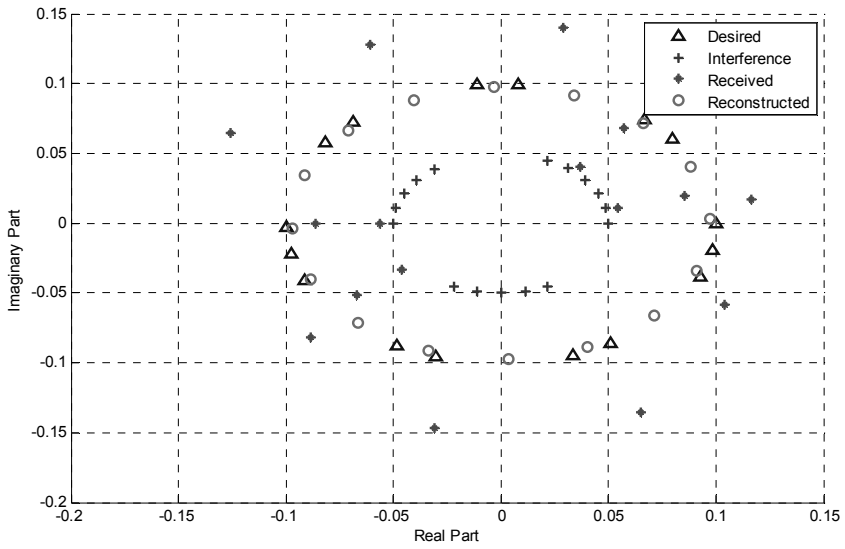


Fig. 8. Quadratic diagram in case of single interferer signal

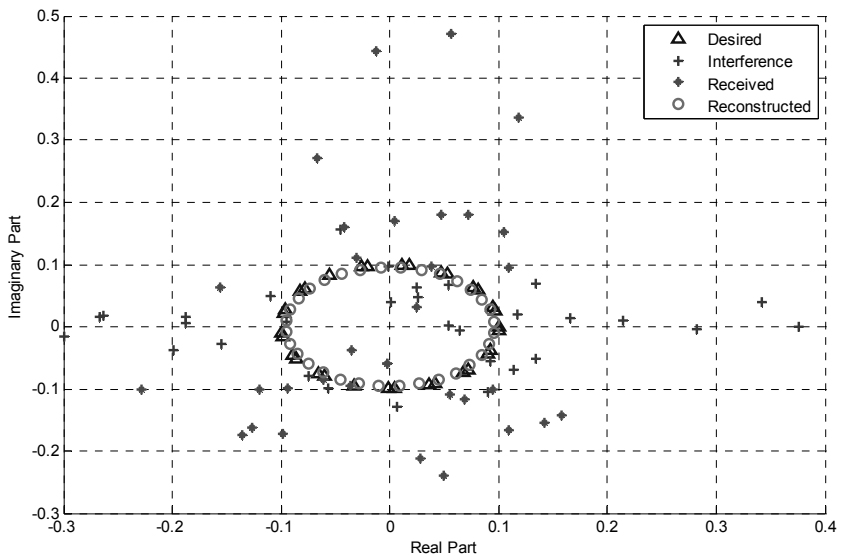


Fig. 9. Quadratic diagram in case of multiple interferer signals

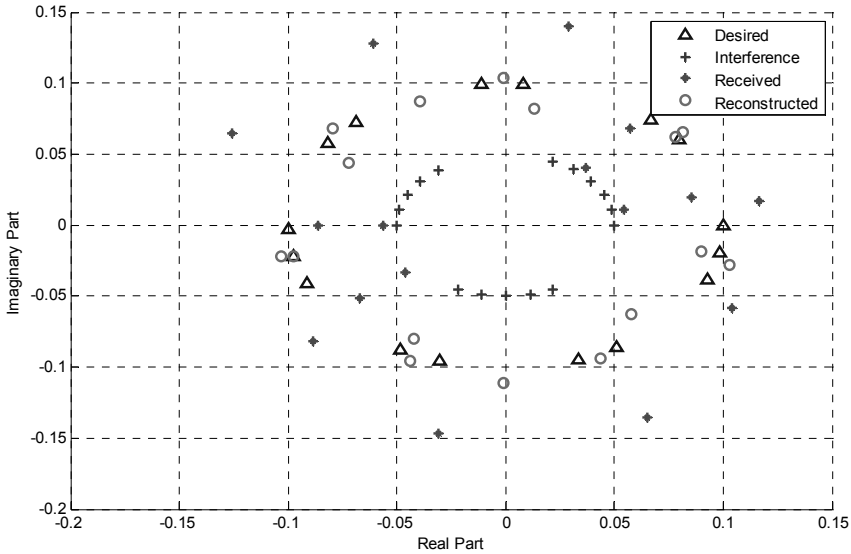


Fig. 10. Quadratic diagrams (complex plane) in case of discarding the interferer signal

- Beam Pattern Characteristics (Beam gain in small angular separation between desired and undesired signals).
- Resulting Signal-to-Interference Ratio SIR.
- Bit Error Rate (BER) behavior with Respect to SINR.
- System Capacity (Number of user in the system).
- The Outage Probability of the System.
- Computational Complexity.
- Convergence Speed.
- Tracking performances

In each case, simulation environment parameters are assumed to realize the system in the case. Overall simulation environments are written using MATLAB code.

4.1 Beam pattern performance

The array response to the signal with direction of arrival θ is given by [5]

$$G(\theta) = \sum_{i=1}^M w_i^* e^{-j\frac{2\pi}{\lambda}(i-1)d \sin \theta} \tag{29}$$

where w_i is the i th value of the weight vector. This array response, $G(\theta)$, can also be represented in a vector form as

$$G(\theta) = \mathbf{w}^H \mathbf{a}(\theta) \tag{30}$$

where \mathbf{w} is the weight vector and H is the Hermitian notation. The beam pattern G_{BP} defined as the magnitude of $G(\theta)$ has the form

$$G_{BP}(\theta) = \left| \mathbf{w}^H \mathbf{a}(\theta) \right| \quad (31)$$

Initially, a simulation is carried out assuming arrival direction of the desired signal at 60° interfering signal arrives from 50° (small separation angle and equal power of the desired signal, which represents a tight condition) and the initial weights vector is taken as the first column of the identity matrix, i.e. $\mathbf{w}(0) = [1, 0, 0, \dots, 0_M]^T$. The results obtained after 1000 iterations, using an adaptive array system with eight antennas. The beam pattern obtained for the conventional Constant Modulus Algorithm (CMA), which is considered as one of the most efficient blind algorithms and the proposed technique. A comparison between these two results is displayed in Fig.11. It is clear that the maximum gain of the main lobe directed toward the desired direction for the proposed hybrid technique is greater than that for the conventional CMA by about 2 dB, and the minimum gain (null) at undesired direction for the proposed technique is less than that for the conventional CMA by 7 dB (better performance). This means that the proposed hybrid algorithm is more efficient in forming the beam pattern. The results are as displayed in Fig. 12 from which it is clear that the directivity of the hybrid algorithm is higher than that of the conventional one, i.e., the former is more capable in distinguishing between neighboring users (a serious problem for conventional blind adaptive beamforming algorithm).

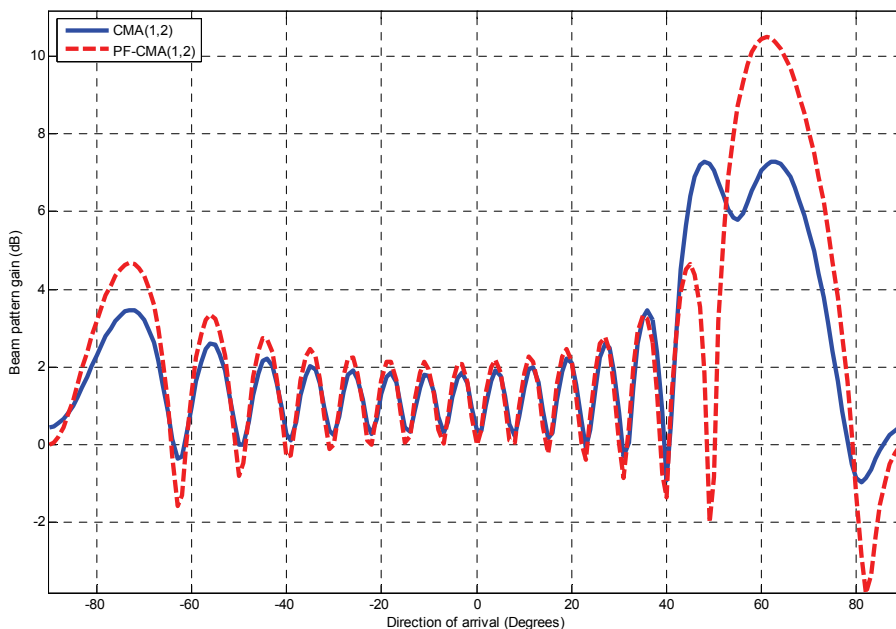
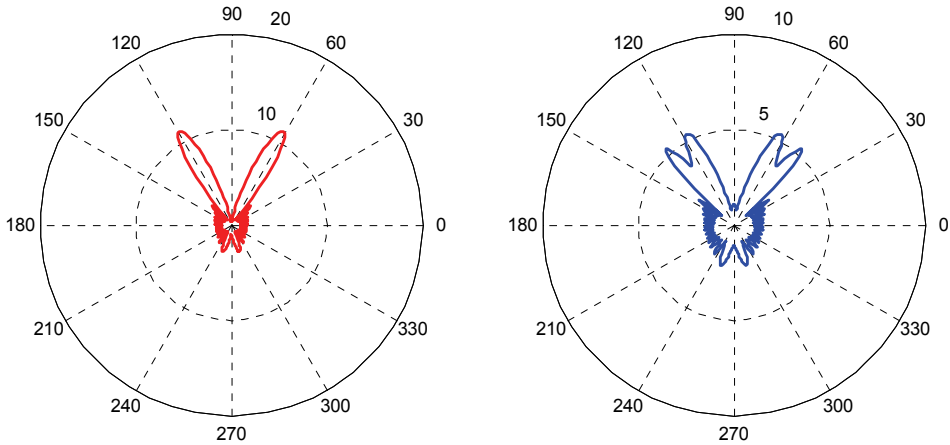


Fig. 11. Beam patterns of CMA and hybrid technique in (dB)



(a) Polar beam pattern of hybrid technique (b) Polar beam pattern of CMA(1, 2)

Fig. 12. Polar beam patterns of CMA and hybrid technique for small angular separation between desired and interfering DOAs

4.2 Signal-to-Interference Ratio (SIR) performance and power budget

The SIR for adaptive array can be written to have the form

$$SIR = \frac{\mathbf{w}^H s_d^2 \mathbf{a}(\theta_d) \mathbf{a}^H(\theta_d) \mathbf{w}}{\mathbf{w}^H \mathbf{R}_I \mathbf{w}} \tag{32}$$

where $\mathbf{a}(\theta_d)$ is the array propagation vector at the desired direction of arrival, s_d is the desired signal sample, and \mathbf{R}_I is the covariance matrix of the interference signal.

The simulation is carried out under the same previous conditions, but with lower noise level. Fig. 13 shows the results. The steady state of the hybrid technique is at about 23 dB while that of the conventional algorithm is less than 6 dB (improvement of more than 17 dB in favor of the proposed technique). The SIR for both algorithms is evaluated as a function of interfering DOA assuming the desired user is at 0°. Fig. 14 indicates a better performance for the hybrid technique in most of the time.

To obtain the power budget in this tight case, i.e., at a smaller angular separation of 10 degrees, we determined the ratio between the gain beam pattern at desired direction, G_d , and the maximum possible gain G_{max} , i.e. G_d/G_{max} . This ratio is 11/16 for the hybrid CMA technique and 5/16 for the conventional CMA, another advantage of the proposed technique (Gain of the power budget more than 3 dB).

4.3 BER behavior with respect to SINR

This part studies the effects of the proposed technique on the required SINR to achieve a specific bit error rate. Throughout this chapter the required BER is assumed to be 10^{-8} because of simulation considerations, since a BER of 10^{-k} needs $10^{(k+1)}$ samples for the simulation results to lie within a confidence interval of 90% [2]. The conventional CMA

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