

Agent-Based Co-Evolutionary Techniques for Solving Multi-Objective Optimization Problems

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1. Introduction

Evolutionary algorithms (EAs) are optimization and search techniques inspired by the Darwinian model of biological evolutionary processes (Bäck et al., 1997). EAs are robust and efficient techniques, which find approximate solutions to many problems which are difficult or even impossible to solve with the use of “classical” techniques. There are many different types of evolutionary algorithms developed during over 40 years of research.

One of the branches of EAs are *co-evolutionary algorithms (CEAs)* (Paredis, 1998). The main difference between EAs and CEAs is the way in which the fitness of an individual is evaluated in each approach. In the case of evolutionary algorithms each individual has the solution of the given problem encoded within its genotype and its fitness depends only on how “good” is that solution. In the case of co-evolutionary algorithms of course there is also obviously solution to the given problem encoded within the individual’s genotype but the fitness is estimated on the basis of interactions of the given individual with other individuals present in the population. Thus co-evolutionary algorithms are applicable in the case of problems for which it is difficult or even impossible to formulate explicit fitness function—in such cases we can just encode the solutions within the individuals’ genotypes and individuals compete—or co-operate—with each other, and such process of interactions leads to the fitness estimation. Co-evolutionary interactions between individuals have also other positive effects. One of them is maintaining the population diversity, another one are “arms races”—continuous “progress” toward better and better solutions to the given problem via competition between species.

Co-evolutionary algorithms are classified into two general categories: competitive and cooperative (Paredis, 1998). The main difference between these two types of co-evolutionary algorithms is the way in which the individuals interact during the fitness estimation. In the case of competitive co-evolutionary algorithms the value of fitness is estimated as a result of the series of tournaments, in which the individual for which the fitness is estimated and some other individuals from the population are engaged. The way of choosing the competitors for tournaments may vary in different versions of algorithms—for example it may be the competition with the best individual from the other species or competition with several randomly chosen individuals, etc.

On the other hand, co-operative co-evolutionary algorithms (CCEAs) are CEAs in which there exist several sub-populations (species) (Potter & De Jong, 2000). Each of them solves

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only one sub- problem of the given problem. In such a case the whole solution is the group of individuals composed of the representants of all sub-populations. Individuals interact only during the fitness estimation process. In order to evaluate the given individual, representants from the other sub-populations are chosen (different ways of choosing such representants may be found in (Potter & De Jong, 2000)). Within the group the given individual is evaluated in such a way that the fitness value of the whole solution (group) becomes the fitness value of the given individual. Individuals coming from the same species are evaluated within the group composed of the same representants of other species.

Sexual selection is another mechanism used for maintaining population diversity in EAs. Sexual selection results from the co-evolution of female mate choice and male displayed trait (Gavrilets & Waxman, 2002). Sexual selection is considered to be one of the ecological mechanisms responsible for biodiversity and sympatric speciation (Gavrilets & Waxman, 2002; Todd & Miller, 1997). The research on sexual selection mechanism generally concentrated on two aspects. The first one was modeling and simulation of sexual selection as speciation mechanism and population diversity mechanism (for example see (Gavrilets & Waxman, 2002; Todd & Miller, 1997)). The second one was the application of sexual selection in evolutionary algorithms as a mechanism for maintaining population diversity. The applications of sexual selection include multi-objective optimization (Allenson, 1992; Lis & Eiben, 1996) and multimodal optimization (Ratford et al., 1997).

In the case of evolutionary multi-objective optimization (Deb, 1999), high quality approximation of *Pareto frontier* (basic ideas of multi-objective optimization are introduced in Section 2) should fulfill at least three distinguishing features. First of all, the population should be "located" as close to the ideal Pareto frontier as possible. Secondly it should include as many alternatives (individuals) as possible and, last but not least, all proposed non-dominated alternatives should be evenly distributed over the whole true Pareto set. In the case of multi-objective optimization maintaining of population diversity plays the crucial role. Premature loss of population diversity can result not only in lack of drifting to the true Pareto frontier but also in obtaining approximation of Pareto set that is focused around its selected area(s), what is very undesirable. In the case of multi-objective problems with many local Pareto frontiers (so called "multi-modal multi-objective problems" defined by Deb in (Deb, 1999)) the loss of population diversity may result in locating only a local Pareto frontier instead of a global one.

Co-evolutionary multi-agent systems (CoEMAS) are the result of research on decentralized models of co-evolutionary computations. CoEMAS model is the extension of "basic" model of evolution in multi-agent system – *evolutionary multi-agent systems (EMAS)* (Cetnarowicz et al., 1996). The basic idea of such an approach is the realization of evolutionary processes in multi-agent system – the population of agents evolves, agents live within the environment, they can reproduce, die, compete for resources, observe the environment, communicate with other agents, and make autonomously all their decisions concerning reproduction, choosing partner for reproduction, and so on. Co-evolutionary multi-agent systems additionally allow us to define many species and sexes of agents and to introduce interactions between them (Dreżewski, 2003).

All these features lead to completely decentralized evolutionary processes and to the class of systems that have very interesting features. It seems that the most important of them are the following:

- synchronization constraints of the computations are relaxed because the evolutionary processes are decentralized—individuals are agents, which act independently and do not need synchronization,
- there exists the possibility of constructing hybrid systems using many different computational intelligence techniques within one single, coherent multi-agent architecture,
- there are possibilities of introducing new evolutionary and social mechanisms, which were hard or even impossible to introduce in the case of classical evolutionary algorithms.

The possible areas of application of CoEMAS include multi-modal optimization (for example see (Dreżewski, 2006)), multi-objective optimization (the review of selected results is presented in this chapter), and modeling and simulation of social and economical phenomena.

This chapter starts with the overview of multi-objective optimization problems. Next, introduction to the basic ideas of CoEMAS systems—the general model of co-evolution in multi-agent system—is presented. In the following parts of the chapter the agent-based co-evolutionary systems for multi-objective optimization are presented. Each system is described with the use of notions and formalisms introduced in the general model of coevolution in multi-agent system. Each of the presented systems uses different coevolutionary interactions and mechanisms: sexual selection mechanism, and host-parasite co-evolution. For all the systems results of experiments with commonly used multi-objective test problems are presented. The results obtained during the experiments are the basis for comparisons of agent-based co-evolutionary techniques with “classical” evolutionary approaches.

2. An introduction to multi-objective optimization

During most real-life decision processes many different (often contradictory) factors have to be considered, and the decision maker has to deal with an ambiguous situation: the solutions which optimize one criterion may prove insufficiently good considering the others. From the mathematical point of view such multi-objective (or multi-criteria) problem can be formulated as follows (Coello Coello et al., 2007; Abraham et al., 2005; Zitzler, 1999; Van Veldhuizen, 1999).

Let the problem variables be represented by a real-valued vector:

$$\vec{x} = [x_1, x_2, \dots, x_m]^T \in \mathbb{R}^m \quad (1)$$

where m is the number of variables. Then a subset of \mathbb{R}^m of all possible (feasible) decision alternatives (options) can be defined by a system of:

- inequalities (constraints): $g_k(\vec{x}) \geq 0$ and $k = 1, 2, \dots, K$
- equalities (bounds): $h_l(\vec{x}) = 0$, $l = 1, 2, \dots, L$

and denoted by \mathcal{D} . The alternatives are evaluated by a system of n functions (objectives) denoted here by vector $F = [f_1, f_2, \dots, f_n]^T$:

$$f_i : \mathbb{R}^m \rightarrow \mathbb{R}, \quad i = 1, 2, \dots, n \quad (2)$$

Because there are many criteria-to indicate which solution is better than the other-specialized ordering relation has to be introduced. To avoid problems with converting minimization to maximization problems (and vice versa of course) additional operator \triangleleft can be defined. Then, notation $\bar{x}_1 \triangleleft \bar{x}_2$ indicates that solution \bar{x}_1 is simply better than solution \bar{x}_2 for particular objective. Now, the crucial concept of Pareto optimality (what is the subject of our research) i.e. so called dominance relation can be defined. It is said that solution \bar{x}_A dominates solution \bar{x}_B ($\bar{x}_A \prec \bar{x}_B$) if and only if:

$$\bar{x}_A \prec \bar{x}_B \Leftrightarrow \begin{cases} f_j(\bar{x}_A) \not\geq f_j(\bar{x}_B) \text{ for } j = 1, 2, \dots, n \\ \exists i \in \{1, 2, \dots, n\} : f_i(\bar{x}_A) < f_i(\bar{x}_B) \end{cases}$$

A solution in the Pareto sense of the multi-objective optimization problem means determination of all non-dominated alternatives from the set \mathcal{D} . The Pareto-optimal set consists of globally optimal solutions and is defined as follows. The set $\mathcal{P} \subseteq D$ is global Pareto-optimal set if (Zitzler, 1999):

$$\forall \bar{x}^p \in \mathcal{P} : \nexists \bar{x}^d \in D \text{ such that } \bar{x}^d \geq \bar{x}^p \tag{3}$$

There may also exist locally optimal solutions, which constitute locally non-dominated set (*local Pareto-optimal set*) (Deb, 2001). The set $\mathcal{P}_{local} \subseteq D$ is local Pareto-optimal set if (Zitzler, 1999):

$$\forall \bar{x}^p \in \mathcal{P}_{local} : \nexists \bar{x}^d \in D \text{ such that } \bar{x}^d \geq \bar{x}^p \wedge \|\bar{x}^d - \bar{x}^p\| < \varepsilon \wedge \|F(\bar{x}^d) - F(\bar{x}^p)\| < \delta$$

where $\|\cdot\|$ is a distance metric and $\varepsilon > 0, \delta > 0$.

These locally or globally non-dominated solutions define in the criteria space so-called local (\mathcal{PF}_{local}) or global (\mathcal{PF}) Pareto frontiers that can be defined as follows:

$$\mathcal{PF}_{local} = \{\bar{y} = F(\bar{x}) \in \mathbb{R}^n \mid \bar{x} \in \mathcal{P}_{local}\} \tag{4a}$$

$$\mathcal{PF} = \{\bar{y} = F(\bar{x}) \in \mathbb{R}^n \mid \bar{x} \in \mathcal{P}\} \tag{4b}$$

Multi-objective problems with one global and many local Pareto frontiers are called *multimodal multi-objective problems* (Deb, 2001).

3. General model of co-evolution in multi-agent system

As it was said, co-evolutionary multi-agent systems are the result of research on decentralized models of evolutionary computations which resulted in the realization of evolutionary processes in multi-agent system and the formulation of model of co-evolution in such system. The basic elements of CoEMAS are environment with some topography, agents (which are located and can migrate within the environment, which are able to reproduce, die, compete for limited resources, and communicate with each other), the selection mechanism based on competition for limited resources, and some agent-agent and agent-environment relations defined (see Fig. 1).

The selection mechanism in such systems is based on the resources defined in the system. Agents collect such resources, which are given to them by the environment in such a way

that “better” agents (i.e. which have “better” solutions encoded within their genotypes) are given more resources and “worse” agents are given less resources. Agents then use such resources for every activity (like reproduction and migration) and base all their decisions on the possessed amount of resources.

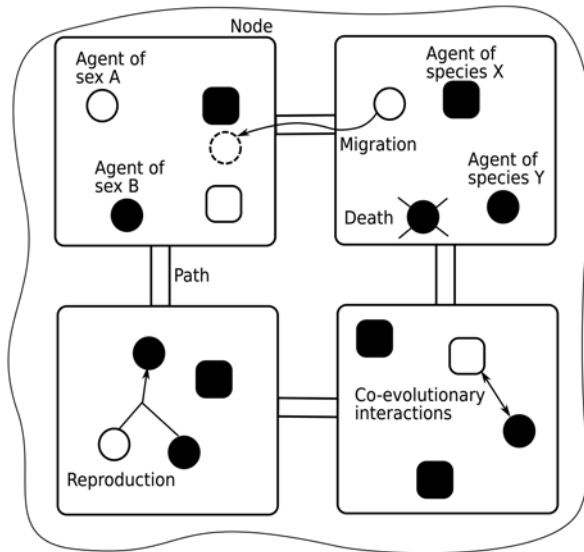


Fig. 1. The idea of co-evolutionary multi-agent system

In this section the general model of co-evolution in multi-agent system (CoEMAS) is presented. We will formally describe the basic elements of such systems and present the algorithm of agent’s basic activities.

3.1 The co-evolutionary multi-agent system

The *CoEMAS* is described as 4-tuple:

$$CoEMAS = \langle E, S, \Gamma, \Omega \rangle \tag{5}$$

where *E* is the environment of the *CoEMAS*, *S* is the set of species ($s \in S$) that co-evolve in *CoEMAS*, Γ is the set of resource types that exist in the system, the amount of type γ resource will be denoted by r^γ , Ω is the set of information types that exist in the system, the information of type ω will be denoted by i^ω .

3.2 The environment

The environment of *CoEMAS* may be described as 3-tuple:

$$E = \langle T^E, \Gamma^E, \Omega^E \rangle \tag{6}$$

where T^E is the topography of environment *E*, Γ^E is the set of resource types that exist in the environment, Ω^E is the set of information types that exist in the environment. The topography of the environment is given by:

$$T^E = \langle H, l \rangle \tag{7}$$

where H is directed graph with the cost function c defined: $H = \langle V, B, c \rangle$, V is the set of vertices, B is the set of arches. The distance between two nodes is defined as the length of the shortest path between them in graph H .

The l function makes it possible to locate particular agent in the environment space:

$$l: A \rightarrow V \tag{8}$$

where A is the set of agents, that exist in $CoEMAS$.

Vertice v is given by:

$$v = \langle A^v, \Gamma^v, \Omega^v, \varphi \rangle \tag{9}$$

A^v is the set of agents that are located in the vertice v , Γ^v is the set of resource types that exist within the v ($\Gamma^v \subseteq \Gamma^E$), Ω^v is the set of information types that exist within the v ($\Omega^v \subseteq \Omega^E$), φ is the fitness function.

3.3 The species

Species $s \in S$ is defined as follows:

$$s = \langle A^s, SX^s, Z^s, C^s \rangle \tag{10}$$

where:

- A^s is the set of agents of species s (by a^s we will denote the agent, which is of species s , $a^s \in A^s$);
- SX^s is the set of sexes within the s ;
- Z^s is the set of actions, which can be performed by the agents of species s ($Z^s = \bigcup_{a \in A^s} Z^a$, where Z^a is the set of actions, which can be performed by the agent a);
- C^s is the set of relations with other species that exist within $CoEMAS$.

The set of relations of s_i with other species (C^{s_i}) is the sum of the following sets of relations:

$$C^{s_i} = \left\{ \xrightarrow{s_i, z^-}: z \in Z^{s_i} \right\} \cup \left\{ \xrightarrow{s_i, z^+}: z \in Z^{s_i} \right\} \tag{11}$$

where $\xrightarrow{s_i, z^-}$ and $\xrightarrow{s_i, z^+}$ are relations between species, based on some actions $z \in Z^{s_i}$, which can be performed by the agents of species s_i :

$$\xrightarrow{s_i, z^-} = \{ \langle s_i, s_j \rangle \in S \times S: \text{agents of species } s_i \text{ can decrease the fitness of agents of species } s_j \text{ by performing the action } z \in Z^{s_i} \} \tag{12}$$

$$\xrightarrow{s_i, z^+} = \{ \langle s_i, s_j \rangle \in S \times S: \text{agents of species } s_i \text{ can increase the fitness of agents of species } s_j \text{ by performing the action } z \in Z^{s_i} \} \tag{13}$$

If $s_i \xrightarrow{s_i, z_k^-} s_i$ then we are dealing with the intra-species competition, for example the competition for limited resources, and if $s_i \xrightarrow{s_i, z_j^+} s_i$ then there is some form of co-operation within the species s_i .

With the use of the above relations we can define many different co-evolutionary interactions e.g.: predator-prey, host-parasite, mutualism, etc. For example, host-parasite interactions between two species, s_i (parasites) and s_j (hosts) ($i \neq j$) take place if and only if $\exists z_k \in Z^{s_i} \wedge \exists z_l \in Z^{s_j}$, such that $s_i \xrightarrow{s_i z_k^-} s_j$ and $s_j \xrightarrow{s_j z_l^+} s_i$, and parasite can only live in tight co-existence with the host.

3.4 The sex

The sex $sx \in SX^s$ which is within the species s is defined as follows:

$$sx = \langle A^{sx}, Z^{sx}, C^{sx} \rangle \tag{14}$$

where A^{sx} is the set of agents of sex sx and species s ($A^{sx} \subseteq A^s$):

$$A^{sx} = \{a : a \in A^s \wedge a \text{ is the agent of sex } sx\} \tag{15}$$

With a^{sx} we will denote the agent of sex sx ($a^{sx} \in A^{sx}$). Z^{sx} is the set of actions which can be performed by the agents of sex sx , $Z^{sx} = \bigcup_{a \in A^{sx}} Z^a$, where Z^a is the set of actions which can be performed by the agent a . And finally C^{sx} is the set of relations between the sx and other sexes of the species s .

Analogically as in the case of species, we can define the relations between the sexes of the same species. The set of all relations of the sex $sx_i \in SX^s$ with other sexes of species s (C^{sx_i}) is the sum of the following sets of relations:

$$C^{sx_i} = \left\{ \xrightarrow{sx_i z^-} : z \in Z^{sx_j} \right\} \cup \left\{ \xrightarrow{sx_i z^+} : z \in Z^{sx_j} \right\} \tag{16}$$

where $\xrightarrow{sx_i z^-}$ and $\xrightarrow{sx_i z^+}$ are the relations between sexes, in which some actions $z \in Z^{sx_j}$ are used:

$$\xrightarrow{sx_i z^-} = \{ \langle sx_i, sx_j \rangle \in SX^s \times SX^s : \text{agents of sex } sx_i \text{ can decrease the fitness of agents of sex } sx_j \text{ by performing the action } z \in Z^{sx_j} \} \tag{17}$$

$$\xrightarrow{sx_i z^+} = \{ \langle sx_i, sx_j \rangle \in SX^s \times SX^s : \text{agents of sex } sx_i \text{ can increase the fitness of agents of sex } sx_j \text{ by performing the action } z \in Z^{sx_j} \} \tag{18}$$

If performing the action $z_k \in Z^{sx_j}$ (which permanently or temporally increases the fitness of the agent a^{sx_j} of sex $sx_j \in SX^s$) by the agent a^{sx_i} of sex $sx_i \in SX^s$ results in performing the action $z_l \in Z^{sx_i}$ by the agent a^{sx_i} and performing the action $z_m \in Z^{sx_j}$ by the agent a^{sx_j} , what results in decreasing of the fitness of agents a^{sx_i} and a^{sx_j} then such relation $\xrightarrow{z_l^- z_m^+}$ will be defined in the following way:

$$\begin{aligned} \xrightarrow{z_l-z_m^-} \xrightarrow{sx_i, z_k^+} = \{ \langle sx_i, sx_j \rangle \in SX^s \times SX^s : \text{agents of sex } sx_i \text{ can increase} \\ \text{(permanently or temporally) the fitness of the agents} \\ \text{of sex } sx_j, \text{ by performing the action } z_k \in Z^{sx_i}, \text{ which} \\ \text{results in performing the action } z_l \in Z^{sx_i} \text{ and the action} \\ z_m \in Z^{sx_j}, \text{ which decrease the fitness of the agents of sex} \\ sx_i \text{ and } sx_j \} \end{aligned} \tag{19}$$

Such relation represents the sexual selection mechanism, where the action $z_k \in Z^{sx_i}$ is the action of choosing the partner for reproduction, the action $z_l \in Z^{sx_i}$ is the action of reproduction performed by the agent of sex sx_i (with high costs associated with it) and the $z_m \in Z^{sx_j}$ is the action of reproduction performed by the agent of sex sx_j (with lower costs than in the case of z_i action).

3.5 Agent

Agent a (see Fig. 2) of sex sx and species s (in order to simplify the notation we assume that $a \equiv a^{sx,s}$) is defined as follows:

$$a = \langle gn^a, Z^a, \Gamma^a, \Omega^a, PR^a \rangle \tag{20}$$

where:

- gn^a is the genotype of agent a , which may be composed of any number of chromosomes (for example: $gn^a = \langle (x_1, x_2, \dots, x_i) \rangle$, where $x_i \in \mathbb{R}$, $gn^a \in \mathbb{R}^k$)
- Z^a is the set of actions, which agent a can perform;
- Γ^a is the set of resource types, which are used by agent a ($\Gamma^a \subseteq \Gamma$);
- Ω^a is the set of informations, which agent a can possess and use ($\Omega^a \subseteq \Omega$);
- PR^a is partially ordered set of profiles of agent a ($PR^a \equiv \langle PR^a, \preceq \rangle$) with defined partial order relation \preceq .

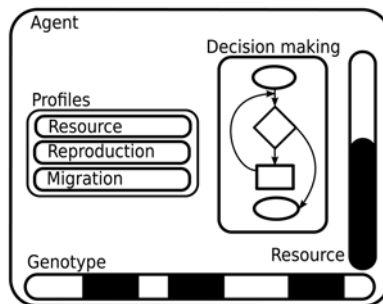


Fig. 2. Agent in the CoEMAS

Relation \preceq is defined in the following way:

$$\preceq = \{ \langle pr_i, pr_j \rangle \in PR^a \times PR^a : \text{realization of active goals of profile } pr_i \text{ has equal or} \\ \text{higher priority than the realization of active goals of profile } pr_j \} \tag{21}$$

The active goal (which is denoted as gl^*) is the goal gl , which should be realized in the given time. The relation \trianglelefteq is reflexive, transitive and antisymmetric and partially orders the set PR^a :

$$pr \trianglelefteq pr \quad \text{for every } pr \in PR^a \quad (22a)$$

$$(pr_i \trianglelefteq pr_j \wedge pr_j \trianglelefteq pr_k) \Rightarrow pr_i \trianglelefteq pr_k \quad \text{for every } pr_i, pr_j, pr_k \in PR^a \quad (22b)$$

$$(pr_i \trianglelefteq pr_j \wedge pr_j \trianglelefteq pr_i) \Rightarrow pr_i = pr_k \quad \text{for every } pr_i, pr_j \in PR^a \quad (22c)$$

The set of profiles PR^a is defined in the following way:

$$PR^a = \{pr_1, pr_2, \dots, pr_n\} \quad (23a)$$

$$pr_1 \trianglelefteq pr_2 \trianglelefteq \dots \trianglelefteq pr_n \quad (23b)$$

Profile pr_1 is the basic profile—it means that the realization of its goals has the highest priority and they will be realized before the goals of other profiles.

Profile pr of agent a ($pr \in PR^a$) can be the profile in which only resources are used:

$$pr = \langle \Gamma^{pr}, ST^{pr}, RST^{pr}, GL^{pr} \rangle \quad (25)$$

in which only informations are used:

$$pr = \langle \Omega^{pr}, M^{pr}, ST^{pr}, RST^{pr}, GL^{pr} \rangle \quad (26)$$

or resources and informations are used:

$$pr = \langle \Gamma^{pr}, \Omega^{pr}, M^{pr}, ST^{pr}, RST^{pr}, GL^{pr} \rangle \quad (27)$$

where:

- Γ^{pr} is the set of resource types, which are used within the profile pr ($\Gamma^{pr} \subseteq \Gamma^a$);
- Ω^{pr} is the set of information types, which are used within the profile pr ($\Omega^{pr} \subseteq \Omega^a$);
- M^{pr} is the set of informations, which represent the agent's knowledge about the environment and other agents (it is the model of the environment of agent a);
- ST^{pr} is the partially ordered set of strategies ($ST^{pr} \equiv \langle ST^{pr}, \trianglelefteq \rangle$), which can be used by agent within the profile pr in order to realize an active goal of this profile;
- RST^{pr} is the set of strategies that are realized within the profile pr —generally, not all of the strategies from the set ST^{pr} have to be realized within the profile pr , some of them may be realized within other profiles;
- GL^{pr} is partially ordered set of goals ($GL^{pr} \equiv \langle GL^{pr}, \trianglelefteq \rangle$), which agent has to realize within the profile pr .

The relation \trianglelefteq is defined in the following way:

$$\trianglelefteq = \{ \langle st_i, st_j \rangle \in ST^{pr} \times ST^{pr} : \text{strategy } st_i \text{ has equal or higher priority than strategy } st_j \} \quad (27)$$

This relation is reflexive, transitive and antisymmetric and partially orders the set ST^{pr} . Every single strategy $st \in ST^{pr}$ is consisted of actions, which ordered performance leads to the realization of some active goal of the profile pr :

$$st = \langle z_1, z_2, \dots, z_k \rangle, \quad st \in ST^{pr}, \quad z_i \in Z^a \quad (28)$$

The relation \preceq is defined in the following way:

$$\preceq = \{ \langle gl_i, gl_j \rangle \in GL^{pr} \times GL^{pr} : \text{goal } gl_i \text{ has equal or higher priority than the goal } gl_j \} \quad (29)$$

This relation is reflexive, transitive and antisymmetric and partially orders the set GL^{pr} . The partially ordered sets of profiles PR^a , goals GL^{pr} and strategies ST^{pr} are used by the agent in order to make decisions about the realized goal and to choose the appropriate strategy in order to realize that goal. The basic activities of the agent a are shown in Algorithm 1.

Algorithm 1. Basic activities of agent a in *CoEMAS*

```

1   $r^\gamma \leftarrow r_{init}^\gamma$ ;          /*  $r_{init}^\gamma$  is the initial amount of resource given to the agent */
2  while  $r^\gamma > 0$  do
3      activate the profile  $pr_i \in PR^a$  with the highest priority and with the active goal
        $gl_j^a \in GL^{pr_i}$ ;
4      if  $pr_i$  is the resource profile then
5          if  $0 < r^\gamma < r_{min}^\gamma$  then; /*  $r_{min}^\gamma$  is the minimal amount of resource needed by the
           agent to realize its activities */
6              |
7              | choose the strategy  $st_k \in ST^{pr_i}$  with the highest priority that can be used to
           take some resources from the environment or other agent;
8              | perform actions contained within the  $st_k$ ;
9          else if  $r^\gamma = 0$  then
10             | execute  $\langle die \rangle$  strategy;
11         end
12     else if  $pr_i$  is the reproduction profile then
13         if  $r^\gamma > r_{min}^{rep,\gamma}$  then; /*  $r_{min}^{rep,\gamma}$  is the minimal amount of resource needed for
           reproduction */
14             |
15             | choose the strategy  $st_k \in ST^{pr_i}$  with the highest priority that can be used to
           reproduce;
16             | perform actions contained within the  $st_k$ ;
17         end
18     else if  $pr_i$  is the migration profile then
19         if  $r^\gamma > r_{min}^{mig,\gamma}$  then; /*  $r_{min}^{mig,\gamma}$  is the minimal amount of resource needed for
           migration */
20             |
21             | choose the strategy  $st_k \in ST^{pr_i}$  with the highest priority that can be used to
           migrate;
22             | perform actions contained within the  $st_k$ ;
23             | give  $r_{min}^{mig,\gamma}$  amount of resource to the environment;
24         end
25     end
26 end

```

In *CoEMAS* systems the set of profiles is usually composed of resource profile (pr_1), reproduction profile (pr_2), and migration profile (pr_3):

$$PR^a = \{pr_1, pr_2, pr_3\} \tag{30a}$$

$$pr_1 \preceq pr_2 \preceq pr_3 \tag{30b}$$

The highest priority has the resource profile, then there is reproduction profile, and finally migration profile.

4. Co-evolutionary multi-agent systems for multi-objective optimization

In this section we will describe two co-evolutionary multi-agent systems used in the experiments. Each of these systems uses different co-evolutionary mechanism: sexual selection, and host-parasite interactions. All of the systems are based on general model of co-evolution in multi-agent system described in Section 3—in this section only such elements of the systems will be described that are specific for these instantiations of the general model. In all the systems presented below, real-valued vectors are used as agents’ genotypes. Mutation with self-adaptation and intermediate recombination are used as evolutionary operators (Bäck et al., 1997).

4.1 Co-evolutionary multi-agent system with sexual selection mechanism (SCoEMAS)

The co-evolutionary multi-agent system with sexual selection mechanism is described as 4-tuple (see Eq. (5)):

$$CoEMAS = \langle E, S, \Gamma = \{\gamma\}, \Omega = \{\omega_1, \omega_2\} \rangle \tag{31}$$

The informations of type ω_1 represent all nodes connected with the given node. The informations of type ω_2 represent all agents located within the given node.

4.1.1 Species

The set of species $S = \{s\}$. The only species s is defined as follows:

$$s = \langle A^s, SX^s, Z^s, C^s \rangle \tag{32}$$

where SX^s is the set of sexes which exist within the s species, Z^s is the set of actions that agents of species s can perform, and C^s is the set of relations of s species with other species that exist in the *SCoEMAS*.

Actions The set of actions Z^s is defined as follows:

$$Z^s = \{die, searchDominated, get, giveDominating, searchPartner, choose, clone, rec, mut, give, accept, selNode, migr\} \tag{33}$$

where:

- *die* is the action of death (agent dies when it is out of resources);
- *searchDominated* finds the agents that are dominated by the given agent;
- *get* is used to get the resources from a dominated agent;

- *giveDominating* gives some resources to the dominating agent;
- *searchPartner* is used to find candidates for reproduction partners;
- *choose* realizes the mechanism of sexual selection – the partner is chosen on the basis of individual preferences;
- *clone* is used to make the new agent – offspring;
- *rec* realizes the recombination (intermediate recombination is used (Bäck et al., 1997));
- *mut* realizes the mutation (mutation with self-adaptation is used (Bäck et al., 1997));
- *give* is used to give the offspring some amount of the parent’s resources;
- *accept* action accepts the agent performing *choose* action as the partner for reproduction;
- *selNode* chooses the node (from the nodes connected with the current node) to which the agent will migrate;
- *migr* allows the agent to migrate from the given node to another node of the environment. The migration causes the lose of some amount of the agent’s resources.

Relations The set of relations is defined as follows:

$$C^{s} = \left\{ \xrightarrow{s, get-} \right\} \tag{34}$$

The relation models intra species competition for limited resources (“-” denotes that as a result of performing *get* action the fitness of another agent of species *s* is decreased):

$$\xrightarrow{s, get-} = \{\langle s, s \rangle\} \tag{35}$$

4.1.2 The sexes

The number of sexes within the *s* species corresponds with the number of criteria (*n*) of the multi-objective problem being solved:

$$SX^s = \{sx_1, \dots, sx_n\} \tag{36}$$

Actions The set of actions of sex *sx* is defined in the following way: $Z^{sx} = Z^s$.

Relations The set of relations of sex *sx_i* is defined as follows:

$$C^{sx_i} = \left\{ \xrightarrow[sx_i, choose+]{give- give-} \right\} \tag{37}$$

The relation $\xrightarrow[sx_i, choose+]{give- give-}$ realizes the sexual selection mechanism (see Eq. (19)). Each agent has its own preferences, which are composed of the vector of weights (each weight for one of the criteria of the problem being solved). These individual preferences are used during the selection of partner for reproduction (*choose* action).

4.1.3 The agent

Agent *a* of sex *sx* and species *s* (in order to simplify the notation we assume that $a \equiv a^{sx,s}$) is defined as follows:

$$a = \langle gn^a, Z^a = Z^s, \Gamma^a = \Gamma, \Omega^a = \Omega, PR^a \rangle \tag{38}$$

In the case of *SCoEMAS* system the genotype of each agent is composed of three vectors (chromosomes): \vec{x} of real-coded decision parameters' values, $\vec{\sigma}$ of standard deviations' values, which are used during mutation with self-adaptation, and \vec{w} of weights used during selecting partner for reproduction ($gn^a = \langle \vec{x}, \vec{\sigma}, \vec{w} \rangle$). Basic activities of agent a with the use of profiles are presented in Alg. 2.

Algorithm 2. Basic activities of agent a in *SCoEMAS*

```

1   $r^\gamma \leftarrow r_{init}^\gamma$ ;
2  while  $r^\gamma > 0$  do
3      activate the profile  $pr_i \in PR^a$  with the highest priority and with the active goal
        $gl_j^i \in GL^{pr_i}$ ;
4      if  $pr_1$  is activated then
5          if  $0 < r^\gamma < r_{min}^\gamma$  then
6               $\langle searchDominated, get \rangle$ ;
7               $r^\gamma \leftarrow (r^\gamma + r_{get}^\gamma)$ ;
8          else if  $r^\gamma = 0$  then
9               $\langle die \rangle$ ;
10         end
11         if  $\langle giveDominating \rangle$  is executed then
12              $r^\gamma \leftarrow (r^\gamma - r_{get}^\gamma)$ ;
13         end
14     else if  $pr_2$  is activated then
15         if  $r^\gamma > r_{min}^{rep,\gamma}$  then
16             if  $\langle searchPartner, choose, clone, rec, mut, give \rangle$  is activated then
17                  $r^\gamma \leftarrow (r^\gamma - r_{give}^{clone,\gamma})$ ;
18             else if  $\langle accept, give \rangle$  is activated then
19                  $r^\gamma \leftarrow (r^\gamma - r_{give}^{accept,\gamma})$ ;
20             end
21         end
22     else if  $pr_3$  is activated then
23         if  $r^\gamma > r_{min}^{mig,\gamma}$  then
24              $\langle selNode, migr \rangle$ ;
25              $r^\gamma \leftarrow (r^\gamma - r_{min}^{mig,\gamma})$ ;
26         end
27     end
28 end

```

$$/* r_{give}^{clone,\gamma} \gg r_{give}^{accept,\gamma} */$$

Profiles The set of profiles $PR^a = \{pr_1, pr_2, pr_3\}$, where pr_1 is the resource profile, pr_2 is the reproduction profile, and pr_3 is the migration profile. The resource profile is defined in the following way:

$$pr_1 = \langle \Gamma^{pr_1} = \Gamma, \Omega^{pr_1} = \{\omega_2\}, M^{pr_1} = \{i^{\omega_2}\}, ST^{pr_1}, RST^{pr_1} = ST^{pr_1}, GL^{pr_1} \rangle \tag{39}$$

The set of strategies includes two strategies:

$$ST^{pr_1} = \{ \langle die \rangle, \langle searchDominated, get \rangle, \langle giveDominating \rangle \} \tag{40}$$

The goal of the profile is to keep the amount of resource above the minimal level.

The reproduction profile is defined as follows:

$$pr_2 = \langle \Gamma^{pr_2} = \Gamma, \Omega^{pr_2} = \{\omega_2\}, M^{pr_2} = \{i^{\omega_2}\}, ST^{pr_2}, RST^{pr_2} = ST^{pr_2}, GL^{pr_2} \rangle \quad (41)$$

The set of strategies includes two strategies:

$$ST^{pr_2} = \{ \langle searchPartner, choose, clone, rec, mut, give \rangle, \langle accept, give \rangle \} \quad (42)$$

The goal of the profile is to reproduce when the amount of resource is above the minimal level needed for reproduction.

The migration profile is defined as follows:

$$pr_3 = \langle \Gamma^{pr_3} = \Gamma, \Omega^{pr_3} = \{\omega_1\}, M^{pr_3} = \{i^{\omega_1}\}, ST^{pr_3} = \{ \langle selNode, migr \rangle \}, RST^{pr_3} = ST^{pr_3}, GL^{pr_3} \rangle \quad (43)$$

The goal of the profile is to migrate to another node when the amount of resource is above the minimal level needed for migration.

4.2 Co-evolutionary multi-agent system with host-parasite interactions (HPCoEMAS)

The co-evolutionary multi-agent system with host-parasite interactions is defined as follows (see Eq. (5)):

$$HPCoEMAS = \langle E, S, \Gamma, \Omega \rangle \quad (44)$$

The set of species includes two species, hosts and parasites: $S = \{host, par\}$. One resource type exists within the system ($\Gamma = \{r\}$). Three information types ($\Omega = \{\omega_1, \omega_2, \omega_3\}$) are used. Information of type ω_1 denotes nodes to which each agent can migrate when it is located within particular node. Information of type ω_2 denotes such host-agents that are located within the particular node in time t . Information of type ω_3 denotes the host of the given parasite.

4.2.1 Host species

The host species is defined as follows:

$$host = \langle A^{host}, SX^{host} = \{sx\}, Z^{host}, C^{host} \rangle \quad (45)$$

where SX^{host} is the set of sexes which exist within the *host* species, Z^{host} is the set of actions that agents of species *host* can perform, and C^{host} is the set of relations of *host* species with other species that exist in the HPCoEMAS.

Actions The set of actions Z^{host} is defined as follows:

$$Z^{host} = \{die, get, give, accept, seek, clone, rec, mut, giveChild, migr\} \quad (46)$$

where:

- *die* is the action of death (host dies when it is out of resources);
- *get* action gets some resource from the environment;
- *give* action gives some resource to the parasite;
- *accept* action accepts other agent as a reproduction partner;
- *seek* action seeks for another host agent that is able to reproduce;

- *clone* is the action of producing offspring (parents give some of their resources to the offspring during this action);
- *rec* is the recombination operator (intermediate recombination is used (Bäck et al., 1997));
- *mut* is the mutation operator (mutation with self-adaptation is used (Bäck et al., 1997));
- *giveChild* action gives some resource to the offspring;
- *migr* is the action of migrating from one node to another. During this action agent loses some of its resource.

Relations The set of relations of *host* species with other species that exist within the system is defined as follows:

$$C^{host} = \left\{ \xrightarrow{host.get-}, \xrightarrow{host.give+} \right\} \tag{47}$$

The first relation models intra species competition for limited resources given by the environment:

$$\xrightarrow{host.get-} = \{\langle host, host \rangle\} \tag{48}$$

The second one models host-parasite interactions:

$$\xrightarrow{host.give+} = \{\langle host, par \rangle\} \tag{49}$$

4.2.2 Parasite species

The parasite species is defined as follows:

$$par = \langle A^{par}, SX^{par} = \{sx\}, Z^{par}, C^{par} \rangle \tag{50}$$

Actions The set of actions Z^{par} is defined as follows:

$$Z^{par} = \{die, seekHost, get, clone, mut, giveChild, migr\} \tag{51}$$

where:

- *die* is the action of death;
- *seekHost* is the action used in order to find the host. Test that is being performed by parasite-agent on host-agent before infection consists in comparing—in the sense of Pareto domination relation—solutions represented by assaulting parasite-agent and host-agents that is being assaulted. The more solution represented by host-agent is dominated by parasite-agent the higher is the probability of infection.
- *get* action gets some resource from the host;
- *clone* is the action of producing two offspring;
- *mut* is the mutation operator (mutation with self-adaptation is used (Bäck et al., 1997));
- *giveChild* action gives all the resources to the offspring—after the reproduction parasite agent dies;
- *migr* is the action of migrating from one node to another. During this action agent loses some of its resource.

Relations The set of relations of *par* species with other species that exist within the system are defined as follows:

$$C^{par} = \left\{ \xrightarrow{par, get-} \right\} \tag{52}$$

This relation models host-parasite interactions:

$$\xrightarrow{par, get-} = \{ \langle par, host \rangle \} \tag{53}$$

As a result of performing *get* action some amount of the resources is taken from the host.

4.2.3 Host agent

Agent *a* of species *host* ($a \equiv a^{host}$) is defined as follows:

$$a = \langle gn^a, Z^a = Z^{host}, \Gamma^a = \Gamma, \Omega^a = \{ \omega_1, \omega_2 \}, PR^a \rangle \tag{54}$$

Genotype of agent *a* is consisted of two vectors (chromosomes): \bar{x} of real-coded decision parameters' values and $\bar{\sigma}$ of standard deviations' values, which are used during mutation with self-adaptation. $Z^a = Z^{host}$ (see Eq. (46)) is the set of actions which agent *a* can perform. Γ^a is the set of resource types used by the agent, and Ω^a is the set of information types. Basic activities of the agent *a* are presented in Alg. 3.

Profiles The partially ordered set of profiles includes resource profile (*pr*₁), reproduction profile (*pr*₂), interaction profile (*pr*₃), and migration profile (*pr*₄):

$$PR^a = \{ pr_1, pr_2, pr_3, pr_4 \} \tag{55a}$$

$$pr_1 \preceq pr_2 \preceq pr_3 \preceq pr_4 \tag{55b}$$

The resource profile is defined in the following way:

$$pr_1 = \langle \Gamma^{pr_1} = \Gamma, \Omega^{pr_1} = \emptyset, M^{pr_1} = \emptyset, ST^{pr_1}, RST^{pr_1} = ST^{pr_1}, GL^{pr_1} \rangle \tag{56}$$

The set of strategies includes two strategies:

$$ST^{pr_1} = \{ \langle die \rangle, \langle get \rangle \} \tag{57}$$

The goal of the *pr*₁ profile is to keep the amount of resources above the minimal level or to die when the amount of resources falls to zero.

The reproduction profile is defined as follows:

$$pr_2 = \langle \Gamma^{pr_2} = \Gamma, \Omega^{pr_2} = \{ \omega_2 \}, M^{pr_2} = \{ i^{\omega_2} \}, ST^{pr_2}, RST^{pr_2} = ST^{pr_2}, GL^{pr_2} \rangle \tag{58}$$

The set of strategies includes two strategies:

$$ST^{pr_2} = \{ \langle seek, clone, rec, mut, giveChild \rangle, \langle accept, giveChild \rangle \} \tag{59}$$

The only goal of the *pr*₂ profile is to reproduce. In order to realize this goal agent can use strategy of reproduction $\langle seek, clone, rec, mut, giveChild \rangle$ or can accept other agent as a reproduction partner $\langle accept, giveChild \rangle$.

The interaction profile is defined as follows:

$$pr_3 = \langle \Gamma^{pr_3} = \Gamma, \Omega^{pr_3} = \emptyset, M^{pr_3} = \emptyset, ST^{pr_3} = \{\langle give \rangle\}, RST^{pr_3} = ST^{pr_3}, GL^{pr_3} \rangle \tag{60}$$

The goal of the pr_3 profile is to interact with parasites with the use of strategy $\langle give \rangle$, which gives some of the host's resources to the parasite.

The migration profile is defined as follows:

$$pr_4 = \langle \Gamma^{pr_4} = \Gamma, \Omega^{pr_4} = \{\omega_1\}, M^{pr_4} = \{i^{\omega_1}\}, ST^{pr_4} = \{\langle migr \rangle\}, RST^{pr_4} = ST^{pr_4}, GL^{pr_4} \rangle \tag{61}$$

The goal of the pr_4 profile is to migrate within the environment. In order to realize such a goal the migration strategy is used, which firstly chooses the node and then realizes the migration. Agent loses some of its resources in order to migrate.

Algorithm 3. Basic activities of agent $a \equiv a^{host}$ in *HPCoEMAS*

```

1  $r^\gamma \leftarrow r_{init}^\gamma$ ;
2 while  $r^\gamma > 0$  do
3   activate the profile  $pr_i \in PR^a$  with the highest priority and with the active goal
    $gl_j^* \in GL^{pr_i}$ ;
4   if  $pr_1$  is activated then
5     if  $0 < r^\gamma < r_{min}^\gamma$  then
6        $\langle get \rangle$ ;
7        $r^\gamma \leftarrow (r^\gamma + r_{get}^{env,\gamma})$ ; /*  $r_{get}^{env,\gamma}$  is the amount of resource given by the
       environment */
8     else if  $r^\gamma = 0$  then
9        $\langle die \rangle$ ;
10    end
11   else if  $pr_2$  is activated then
12     if  $r^\gamma > r_{min}^{rep,\gamma}$  then
13       if  $\langle seek, clone, rec, mut, giveChild \rangle$  is performed then
14          $r^\gamma \leftarrow (r^\gamma - r_{giveChild}^\gamma)$ ;
15       else if  $\langle accept, giveChild \rangle$  is performed then
16          $r^\gamma \leftarrow (r^\gamma - r_{giveChild}^\gamma)$ ;
17       end
18     end
19   else if  $pr_3$  is activated then
20      $\langle give \rangle$ ;
21      $r^\gamma \leftarrow (r^\gamma - r_{give}^\gamma)$ ;
22   else if  $pr_4$  is activated then
23     if  $r^\gamma > r_{min}^{mig,\gamma}$  then
24        $\langle migr \rangle$ ;
25        $r^\gamma \leftarrow (r^\gamma - r_{min}^{mig,\gamma})$ ;
26     end
27   end
28 end

```

4.2.4 Parasite agent

Agent a of species par ($a \equiv a^{par}$) is defined as follows:

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